A Theory of Minimalist Democracy*

Chris Bidner† Patrick Francois‡ Francesco Trebbi§

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Abstract

Democracies in which political elites hold and respect elections, yet do not extend related freedoms (civil liberties, free press, rule of law, etc.) that empower the non-elite, are empirically relevant, but imperfectly understood. What motivates the elite to respect the electoral wishes of a weak non-elite in such systems? We lay out a formal model that sheds light on this, and related questions raised by such minimalist democracies. In the model, competitive elections mitigate coup threats arising from within the elite because of imperfectly transferable office rents. We characterize the conditions under which such a power-sharing agreement is supported i.e. when those out of power do not want to seize it, and when those in power are willing to cede it. We highlight the benefits of using elections for power-sharing, arguing that it strengthens such agreements by removing the mutually beneficial temptation to ‘forgive and forget’ previous violations. We use the model to help understand democratic transitions and empirically demonstrate one of its key implications, that reduced transferability of office rents induce transitions to minimalist versions of democracy.

Keywords: Democratic theory; Minimalist democracy; Political transitions; Autocracy
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†Simon Fraser University, Department of Economics, cbidner@sfu.ca
‡CIFAR, CEPR and University of British Columbia, Vancouver School of Economics, patrick.francois@ubc.ca
§CIFAR, University of British Columbia, Vancouver School of Economics, and NBER, francesco.trebbi@ubc.ca
1 Introduction

Many countries that hold elections systematically lack other key elements of fully-fledged democracies – civil liberties, right to vote, a free press, the rule of law, a constrained executive branch. Occasionally, elections in these countries are farcical affairs largely devoid of meaning – a recent example: North Korea in 2014. But in a good number of other instances, though little else from a list of widely shared democratic attributes appears, elections with some meaning do take place. To be sure, these may still be highly restrictive affairs, but fierce electoral competition does take place – a recent example: Nigeria in 2015.

As Diamond (2002) argues, elections like these meet Schumpeter’s (1942) procedural definition for “minimalist democracies” and indeed can be found in all parts of the developing world: in the Americas – The Dominican Republic, Ecuador, El Salvador, Haiti, Honduras, Nicaragua, Panama. In Asia – Indonesia, Nepal, Moldova, Mongolia. In Sub-Saharan Africa this procedural definition applies to a large share countries, including Kenya, Malawi, Nigeria, Tanzania, Uganda, Zambia.

The elements of democracy that these minimalist democracies lack are precisely those enabling the masses to exert influence on leaders. Thus, it is not surprising to find that such democracies tend to fail to deliver significant material broad-based benefits to their citizens. For instance, in the case of Sub-Saharan Africa, Van de Walle (2003, p.36) discusses how “Political freedoms and civil rights may be formally recognized but are imperfectly observed in practice...Human rights abuses are not uncommon, even if the worst abuses are rarer than in the authoritarian past. A nominally free press is harassed in myriad ways, and the government retains a radio monopoly. Certain groups, notably key members of the executive branch and the military may, in effect, be above the law. The judiciary is officially independent, but it is poorly trained, overworked and easily compromised.”

These regimes present a conceptual challenge because of their counterintuitive nature. If the power of the masses is sufficiently undermined that they are unable to impose their interests upon their leaders, then they are surely similarly powerless to ensure that election results are respected. But then what does motivate election losers to cede power in minimalist democracies? Why are elections held in the first place? Understanding such questions is an important step in understanding the nature of minimalist (i.e. merely electoral) democracies – the conditions under which they emerge and regress, why, and whether they are merely a transitional phase on the way to consolidated democracy or a meaningful and long-lived political type in itself.

This paper develops a model designed to shed light on such issues. To make our point starker, we take an extreme position whereby the non-elite pose no threat to the elite. In-

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1See Dahl (1971) for a prominent discussion of the several elements comprising such list and the dimensionality reduction exercise of focusing on contestation and inclusiveness.

2Diamond (2002, p.21) “Some measure democracy by a ‘minimalist’ standard like Joseph Schumpeter’s: a political system in which the principal positions of power are filled ‘through a competitive struggle for the people’s vote.’”

3Bratton and Van de Walle (1997) who date meaningful elections in Africa to the start of the third wave of democratization there in the 1990s. Between 1990 and 1994, 38 countries in Sub-Saharan Africa out of 47 experienced competitive contests and 11 incumbents were replaced through them. Abstracting from the African case, we present systematic motivating evidence in Section 2.
stead, we focus on within-elite conflict. We also show how this theoretical framework is useful in matching important empirical regularities in democratic theory, including the systematic lack of redistribution after democratizations, the systematic emergence of electoral contestation in hybrid regimes (a novel fact that we establish in this paper), and the political resource curse.

It has already been established that imperfect transferability (or non-divisibility) of the spoils of office may render coups inevitable. Such coups are costly, so elections are a means to share power over time (Fearon 1995, Przeworski 1991). But the questions of how and when such power-sharing agreements are self-enforcing and what advantages elections have over alternative means of sharing are not well understood. To effectively share power via elections, two conditions must be met. First, those not in power must not want to seize control via a coup. This requires that there is sufficient flexibility in being able to distribute office rents to adequately compensate those not in power. Second, those in power must peacefully leave office when required. The latter condition is more complex – without a threat emanating from citizens, a refusal to step down when losing must alter the terms of the power-sharing agreement if it is to be dissuaded. Facing a recalcitrant leader, the only recourse a non-leader possesses is to mount a coup, but this punishment imposes a cost on themselves. We show that pursuing punishment is Pareto dominated by an agreement to ‘forgive and forget’– to return to the original power-sharing agreement as if the violation had not occurred. In this sense the credibility of punishment (and thus the incentive to avoid it) is undermined.

But this is precisely why elections are useful in supporting power-sharing. A candidate's popularity among voters is intuitively diminished if they violate an election. As such, their prospects for sharing power via elections in the future change. The possibility of forgiving, forgetting, and returning to the original power-sharing agreement is impaired or may even vanish. Specifically, diminished future electoral prospects push a violator toward optimally abandoning elections. This is particularly costly when there is insufficient flexibility in allocating the spoils of office, since doing so invites costly coups. In short, the credibility of the punishment to be imposed on violators is enhanced by vesting control over the mechanics of the power-sharing agreement to citizens. Voters act as an external party that turns the terms of the power-sharing agreement against violators. Thus, although the non-elite are powerless in our model, they are by no means superfluous in their role as voters.

The model has implications for furthering specific dimensions of the democratization process. It helps understanding top-down transitions to democracy in which there seemed to be no active agitation from the masses (such as the well documented elite-driven electoral wayposts of Ghana in 2000, Cabo Verde in 1991, and Taiwan in 1996). By considering the threat arising from within the elite, we introduce a role for the transferability of office rents. Whilst it is true that greater transferability enhances the scope for the elite to come to mutually beneficial agreements, we show how the incentive to respect elections – and thus the existence of minimalist democracy – is actually jeopardized by sufficiently transferable office rents.

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This feature is crucial in allowing us to match the well-known empirical regularity whereby greater access to resource wealth – a proxy for the transferability of office rents – promotes autocracy via a mechanism that is distinct from existing explanations. Moreover, our model allows us to make a finer prediction: natural resource windfalls promote the elections component of democracy. We produce empirical support on this in Section 4 as well as studying the systematic patterns of emergence of minimalist democracies in Section 2.

The present paper is related to a number of others that have analyzed the means by which democracy can be “self-enforcing”. Fearon (2011), and Egorov and Sonin (2014) both study this question. However, in both models, enforcement is based on threats from the masses, as a leader not stepping down faces dissent from the street. Relative to our paper, these approaches face the challenge of explaining why it is that a populace can be so important for determining whether a leader continues to hold on to power, while at the same time is not able to assert its will to obtain the other freedoms and benefits accruing to voters in full democracies. Relative to their analyses, our paper faces the challenge of explaining why voters have any role to play at all given that all power is determined by the actions of elites. As will be seen, it is precisely the voters’ lack of a direct stake in violent conflicts determining leadership change which make power alternations that rest on the voters’ say so credible. As argued in Svolik (2012), these are not unimportant threats, in fact coups d’état are the main threat to continued leadership faced by leaders in elite-centred regimes.5

Przeworski (2005, 2006) and Benhabib and Przeworski (2006) also analyze the self-enforcing aspect of a leader’s decision to leave office following an electoral loss. In these analyses the cost of not stepping down is that the leader must become a dictator (and this leads to fewer freedoms – and perhaps status – for the leader). Facing these costs, the leader prefers to respect election outcomes and step down. Our theory starts down a similar path to these papers, but adds the following insight. In general, there is no reason for dictatorship to be a permanent state. A leader may refuse to step down, and hence enter in to the “punishment” highlighted by these papers. But since this phase is both costly to the leader and to the insiders – as they must now challenge for leadership through violence – it should be possible for them to mutually agree to reverting to peaceful alternation. The possibility of renegotiation is not contemplated in any of these analyses, but would seem to substantially weaken them. Formally exploring it in our setting gives rise to an explanation for the specific role that voters and elections play in minimalists democracies.

The seminal analyses of democratization by Acemoglu and Robinson (2001) and Boix (2003) differ from the analysis here in two important ways. Firstly, they provide theories of a much more complete form of democratization than is our focus here. For them, democratization is a movement away from elite rule to essentially a rule of the masses. So, theirs is a theory of transition from autocracy to full and representative democracy. Second, as in the cases above, enforcement of democratic rule rests on citizens’ threats of rebellion. As a direct consequence, democracy, which is in fact median voter rule, would imply policies and rules that directly serve the interests of the non-elites. This clearly cannot explain the minimalist democracies of the world, which by definition do not include any of the other accompani-

5See Kendall-Taylor and Frantz (2014), Geddes (2003), Svolik (2009) and Ezrow and Frantz (2011) for further analysis of turnovers in autocracies and empirical evidence in support of this statement.
ments to elections. This also cannot explain why democratizations – in the minimalist sense – do not seem to be accompanied by or followed by substantive changes in redistribution or systematic improvements on a vast range of public goods beneficial to the masses. Again, this arises naturally in our framework where the non-elite have no power to impose their policy will on the elite. We present a substantial amount of evidence, much of which novel, in Section 2.

A different set of papers have sought to explain the use of elections by a powerful elite based on informational grounds. A reason for holding elections would be to gain information useful in precluding costly conflicts. Przeworski (1999) explores such a role for elections in revealing the strength of support for contesting parties. If relative support at the ballot box informs of the relative strength in violent conflict, then it may be a cheaper and self-enforcing means of inducing turnover. The uncertainty of support from the masses plays a key role there, so such an explanation again hinges on the masses being able to exert influence. But as argued already, if the rank and file’s influence is that great, this begs the question of why non-elites are not able to get other broad democratic outcomes – like rule of law, and respect for civil liberties. Our focus here, in contrast, is on extremely weak non-elites.

Some of the rudiments of the model developed here are present in Francois, Rainer, and Trebbi (2015). In particular, the transfers available to dissuade threats from a coup capable elite are modeled in a similar manner. But the main focus of the present paper is not available there, namely the use of elections to decide on the identity of the leader. This is because that paper is restricted to the part of the parameter space where elections are dominated by transfers, and hence where autocracy is the chosen form of elite rule. As will be shown here, where we consider the full set of possibilities, when transferrable rents are in a lower range, minimalist democracy becomes a dominant form of governance for all of the elite. This identification of the parametric limits of minimalist democracy also yields the paper’s empirical implications.

6Acemoglu, Naidu, Restrepo, and Robinson (2013) for recent evidence of lack of redistribution.
7Tucker and LaGatta (2015) explain how elections can be enforced – in the sense of leaders readily stepping down without being mechanically constrained to do so. In weak polities their explanation rests on election results signalling the popularity of a regime. Unlike our analysis, the non-elite there do have the power to bring down the government. Coordinated actions of the rank and file can lead to the ousting of unpopular regimes, and elections provide signals of incumbent popularity and facilitate coordination. Though not focused on elections, a recent paper by Casper and Tyson (2014) presents a similar signaling model, which differs in its focus on coups – and hence threats from the elite – as the source of regime instability. Opportunities to topple the current leader are signalled by non-elite protests, so that the elite may act on this and move against leaders who have been signalled as weak. Rozenas (2012) is another example of a signalling role for elections, and again rests on threats of revolutions toppling regimes. Malesky and Schuler (2010) also see elections as a device for autocratic leaders to gauge support for potential rivals in the general population. These authors go further in assessing the potential fall-out for a leader unable to manipulate either the running of or tallying of the electoral results. A question that all such approaches which rest enforcement on the potential of rebellion from the masses cannot readily explain is why if the non-elite are so instrumental in bringing down governments are they so poorly accommodated by the actions of those governments.
8Magaloni (2008) also explains why strong elites who are not facing direct threats to power from non-elites would want to use elections to decide paramount positions. Similar to here, leaders can dissuade coup attempts by transferring resources to threatening elites. However, a leader may promise transfers to insiders only to fail to deliver once the insider has joined the regime. She explains how single, and multi-, party elections can help leaders overcome this
A small literature has also analyzed the phenomenon of purely elite-driven democratizations. These papers are able to explain why policy may only move in isolated dimensions in favor of the non-elite. According to these theories the elites precipitate franchise extension on their own terms, and for their own ends, remaining largely in control of the state apparatus. Lizzieri and Persico (2006) explain why a small elite might want to extend the franchise in order to overcome the problem of temporarily decisive groups from within the elite using leadership to redistribute to themselves instead of providing public goods (which are more efficient for the elite as a whole). Extending the franchise increases the equilibrium provision of public goods, which they argue happened in 19th century Britain. Llavador and Oxoby (2005), similarly applied to the 19th century, also studies franchise extension. There, a faction of the elite (industrialists) favour franchise extension, i.e. democratization, in order to obtain policies that they prefer at the expense of another elite faction (landlords) who they cannot defeat otherwise. Both of these papers are similar to ours in their focus on an elite voluntarily extending decision power on leadership identity to the non-elite. In each of these, the extent of the franchise granted to non-elites, or the identity and policy interests of the non-elite play key roles in influencing the form of policy. As such, they are concerned with polities where governance is, at least partly, reflective of the interests of the non-elite, and in explaining shifts in policy that happened in the countries where extension occurred. These would not seemingly apply to the non-redistributive, elite-catering electoral democracies that proliferate in weakly institutionalized settings today.

Wantchekon and Neeman (2002) similarly analyze a set-up where a powerful elite chooses to implement democracy. Again, there, the non-elite have no power to force their demands. They have in common with the present paper the position that elections provide a type of randomization device that allow the elite to undertake power sharing. A major difference is, once again, that the election results obtained there do not need to be self-enforcing, but are binding on the participants. A further implication of their analysis is that the degree of elite expropriation also falls, that governance improves, benefiting the non-elites. Our explanation imposes no such requirement, and is thus more immediately consistent with observed minimalist democracies.

The paper is organized as follows. Section 2 documents the empirical relevance of minimalist, purely electoral democracies, and their features. There we assess how many of the hybrid regimes that populate the intermediate or “gray zone” (Diamond, 2002) in democratic transitions are in fact minimalist democracies and their systematic emergence from autocratic regimes. We also document the resilience of minimalist democracies and that it is not the case that minimal democracy is simply a stepping-stone inevitably leading to full democracy. Section 3 presents the model. Section 4 analyzes the role of elections and history dependence, and adds empirical implications. Section 5 concludes.
2 Motivating Facts

In the previous section we briefly motivated our analysis by emphasizing how prevalent less than consolidated democracies – i.e. regimes in the “gray zone” – are. As reported in Figure 1, they cover a sizeable share of polities worldwide and over time.

This section has the goal of providing a set of stylized facts justifying our focus on electoral (minimalist) democracies. We show that: 1. Minimalist democracies exist almost exclusively in the gray zone; 2. Minimalist democracies are the overwhelming point of departure from non-democracy; 3. Minimalist democracies can be persistent over time. To the best of our knowledge these stylized facts are new to the literature on democratic theory.

**Fact 1:** Less than consolidated democracies are predominantly minimalist, in the sense of satisfying electoral competitiveness requirements but little more. This could be readily observed in the raw data, were detailed disaggregated measures of political features in fact available. Ideally one would require, at the very least, specific scores for both competitiveness and inclusiveness of the political process, the two main factors in Dahl’s famous decomposition of the democratic state.

The Polity IV project (Marshall, 2013), a standard reference in the measurement of political regimes characteristics, offers such decomposition, producing scores for competitiveness of executive recruitment (XRCOMP), openness of executive recruitment (XROPEN), limitations on the executive authorities (XCONST) and inclusiveness of political participation (PARCOMP) among different groups in society. An unambiguous interpretation of the Polity IV subdimensions comes from Goldstone, Bates, Epstein, Gurr, Lustik, Marshall, Ulfelder, and Woodward (2010) – that paper’s authors include two of the original Polity principal investigators – explicitly reporting that there are: “two variables in the Polity data set that roughly correspond to the two dimensions Dahl (1971) uses to characterize modern forms of government. We use Polity’s scale for the openness of executive recruitment (EXREC) as a measure of contestation and Polity’s scale of the competitiveness of political participation (PARCOMP) to capture variation in the degree and forms of inclusiveness.” EXREC is the executive recruitment concept variable whose main components are XRCOMP and XROPEN.9 PARCOMP explicitly indicates exclusion from participation among its criteria, by marking as criteria the exclusion of “substantial groups (20% or more of the adult population) from participation” and whether “large classes of people, groups, or types of peaceful political competition are continuously excluded from the political process” (Marshall, 2013, p.26). Polity IV also offers an aggregate measure of the overall degree of democracy in a country, specifically through its revised Polity 2 score, which cumulates the full set of sub-dimensions on a discrete scale of democracy increasing from −10 to 10.10

By looking at which levels of the Polity 2 score (from less democratic to more democratic) the different features of competitiveness and inclusiveness emerge, one can garner a first in-

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9We will focus on the component variables as opposed to the concept variables in what follows, in order to focus on the most disaggregated level possible.

10Although some subcomponents of Polity 2 load somewhat nonlinearly on Polity 2 (for example when it comes to XCONST), XROPEN, XRCOMP, PARCOMP load linearly on the overall score, so none of the results on contestation and inclusiveness reported below hinge on nonlinear loadings of these subcomponents. For details see http://www.systemicpeace.org/inscr/p4manualv2012.pdf
dication of along what dimensions the process of democratic development typically unfolds. It is easy to show that electoral competitiveness emerges systematically earlier than political inclusiveness. Table 1 considers three different country-year subsamples of the Polity 2 data: consolidated democracies (with scores above 8); less than consolidated democracies with scores above 0 but less than 8; less than consolidated autocracies (with score between −5 and 0). It then evaluates how many of the countries within each of the three subgroups reach fully democratic scores for three different dimensions: Competitive elections, coded as 1 if XRCOMP = 2 (transitional arrangements between selection, ascription and/or designation, and competitive election) or 3 (election), and 0 otherwise. Inclusive political process, coded as 1 if PARCOMP = 4 (transitional arrangements to fully politically competitive patterns of all voters) or 5 (competitive: alternative preferences for policy and leadership can be pursued in the political arena.), and 0 otherwise. Executive constraints, coded as 1 if XCONST = 5 (substantial limitations on executive authority) or higher, and 0 otherwise.

Table 1 tries to capture which dimensions of democracy ‘mature’ first. Quite intuitively, consolidated (mature) democracies fare as well in terms of competitive elections as in terms of limitations on the executive authorities and inclusiveness of political participation. Less-than-consolidated democracies – i.e. regimes in the gray zone – fare almost as well as consolidated democracies in terms of competitive elections (XRCOMP). However, regimes in the gray zone fare much worse in terms of limitations on the executive authority (XCONST) and on inclusiveness of political participation (PARCOMP). Weak autocracies finally lose the competitive elections. Using an alternative, but much coarser measure for electoral competitiveness, defined based on the openness of executive recruitment (XROPEN = 4, i.e. open executive recruitment), produces similar patterns. In synthesis, electoral competition is the predominant democratic feature in the gray zone.

In Figure 2 we report the nonparametric representation by local polynomial of the relationship between a dummy for competitiveness of executive recruitment and the overall Polity 2 score in the dashed line. It is evident that competitiveness arises much earlier in the process of democratic consolidation than the same line but for political inclusiveness (in solid). In Figure 3 we again report the nonparametric representation by local polynomial of the relationship between a dummy for competitiveness of executive recruitment and the overall Polity 2 score in the dashed line. And again competitiveness arises much earlier in the process of democratic consolidation than executive constraints (in solid). In Figures 4, 5, and 6 we repeat the analysis, but controlling for country and year fixed effects using semiparametric methods. The competitiveness of executive recruitment emerges at Polity 2 levels around 0 and significantly differently (based on 95% country-clustered confidence bands) than political inclusiveness or executive constraints, which both appear more frequently later on in the democratic consolidation process.

**Fact 2:** **Minimalist democracies are the point of departure from non-democracy.** This second feature of the data is illustrated by focusing on events of democratization and reporting which democratic features emerge at the onset. Acemoglu, Naidu, Restrepo, and Robinson (2013) produce a detailed list of 122 democratizations and of 71 democratic reversals for 175 countries over the 1960-2010 period, which we employ in an event study type of analysis. The authors provide a convincing discussion of the advantages their classification of events rel-
ative to other extant studies (for example the forward-looking classification of Papaioannou and Siourounis, 2008).

The empirical approach we follow is straightforward. For each variable considered in the event study, we partial out year and country fixed effects and normalize the residual mean level 5 years before a democratization (or reversal) to 0. In each figure, the democratization event takes place at $t = 0$ and the behavior of the variable is plotted in a window around it.\footnote{We thank an anonymous referee for suggesting this event study approach and for suggesting this exhaustive set of empirical checks.} For example we can follow the behavior of contestation and inclusiveness around events of institutional change. The conditioning on year and country fixed effects ensures the dynamics we report are not biased by unobserved heterogeneity, composition effects, and global trends, all issues emphasized by Acemoglu et al. (2013) as particularly relevant in this empirical setting.

In Figure 7 we report the behavior around democratizations of electoral contestation and in Figure 8 of inclusiveness. Competitive elections, as defined above, clearly jump at democratization, with a sharp, almost discontinuous increase when the country moves out of nondemocracy. Inclusiveness is instead characterized by a much smoother behavior at $t = 0$. While the data also indicate an increased incidence of inclusive politics at $t = 0$, such increase is about 2/5 in magnitude of the increase in competitive elections, and only after 15 years of inclusive politics do the two variables reach comparable levels of incidence.\footnote{Incidentally, reproducing the event study analysis for executive constraints reports an effect closer to contestation than inclusiveness. This is in line with what reported above.} Hence, contestation systematically leads inclusiveness and countries do not immediately move to a Meltzer and Richard’s type of fully representative democracy at onset, one where the political voice of the median voter may be heard. The lack of empirical support for the Meltzer and Richard’s logic to democratization can be further illustrated by focusing on the behavior of after tax income inequality around democratization. A basic prediction for the theory is that the after tax Gini coefficient should be lower as a country transitions from nondemocracy to democracy. In Figure 9, where we employ after tax Gini from Solt (2014) Standardized World Income Inequality Database, there is no evidence of any break in Gini levels at $t = 0$, if anything the level of inequality increases smoothly over time.

Other institutional features which might be correlated with representation appear also to lag electoral competition. Figure 9 also reports the behavior of the Freedom House civil liberties index (rescaled to indicate maximum level of civil liberties with 1 and minimum with 0). At democratization this particular measure of civil rights attributed to the general population does appear to follow a pattern similar to inclusiveness, smoothly increasing over time after $t = 0$.\footnote{Reproducing the event study analysis for Freedom House political rights index reports an effect qualitatively close to what shown for contestation at $t = 0$. The definition used for political freedom in the Freedom House conflates contestation and inclusiveness and is coarser than the one presented in Polity IV.}

It would be unwarranted to rule out any role for social conflict and rebellion threats in a theory of democracy. The events of the Arab Spring of 2011 are an obvious counterexample of their importance. However, our theory relies on a different mechanism which just may happen to be more empirically salient. To justify our focus on minimalist democracies that
leave little room to pressure from outside the elite, in Figure 9 we report the behavior around
democratization of social unrest measured with a dummy variable for revolutions, demon-
strations, revolts, or strikes from Banks (2015) Cross-National Time-Series Data Archive. The
data do not seem to overwhelmingly indicate social conflict as main precursor of democra-
tizations, or at least that no overwhelming empirical smoking gun is present to suggest our
focus is unwarranted. Social unrest appears marginally higher before democratizations, but
the amount of variation in social unrest appears quantitatively minimal comparing before
and after democratizations, or even relative to reversals (as reported below). Alternative mea-
sures of unrest are not abundant, but when using information on coups from the University of
Illinois’ Cline Center for Democracy Coup D’état Project a similar lack of stark discontinuities
at $t = 0$ is evident.

It is instructive to focus on reversals, i.e. movements into non-democracy. We report this
analysis in Figure 10, 11 and 12, in fashion analog to Figures 7, 8 and 9. Inclusiveness appears
on a downward trend well before reversals at $t = 0$, with electoral competition being the last
feature to be removed. Income inequality appears again unaffected at reversal. Interestingly
civil liberties also tend to present a sharper erosion around reversals.

**Fact 3: Minimalist democracies are non-ephemeral.** This third feature of the data is illus-
trated by focusing on regime transitions. Again, in order to maintain the analysis as trans-
parent as possible, we focus on raw transition matrices across years. Given our definitions
of competitive and inclusive politics indicators above, we define the following four states:
Non-democracy if Competitive elections = 0 and Inclusiveness = 0. Minimalist democracy if
Competitive elections = 1 and Inclusiveness = 0. Alternative democracy if Competitive elec-
tions = 0 and Inclusiveness = 1. Representative democracy if Competitive elections = 1 and
Inclusiveness = 1. The empirical frequencies of the transitions from year $t-1$ to $t$ in the post-
1945 period are reported in Table 2. Focusing on the minimalist democracy state we observe
a year-on-year likelihood of persistence in this state of 92%, which underscores a substantial
level of persistence. In Table 3 report the same data expressed as conditional on a transition
happening between $t-1$ and $t$. Here again the evidence points at minimalist democracy as
being the most likely transition state out of non-democracy. We also reproduced the tran-
sition analysis using different measures for competitive elections (using only XRCOMP = 3)
and inclusive politics (using only PARCOMP = 5) with very similar results.

In terms of length of the spells under the four states described above (and ignoring censor-
ing), the average length of spells under minimalist democracy is 9 years, under representative
democracy is 24 years, under non-democracy is 24 years, and under alternative democracy
is 8 years.

The evidence so far shows that exit from autocracy entails a gradual process of institu-
tional change, early on through competitive elections for authority recruitment and, only sec-
ondarily, through guaranteeing inclusion of other political agents (the poor, for instance). It
remains to be shown what are typical triggers of democratizations and whether they primar-
ily affect the presence of competitive elections as the evidence above suggests. We formalize
this issue next.
3 Model

3.1 Basic Setup

Consider an infinite horizon discrete time economy populated by two types of agents: citizens and the elite. At each date $t$ there are two elites, one of which is the leader and the other the insider. Apart from the roles they assume at a given date, members of the elite are otherwise symmetric.\(^{14}\)

At the start of the period, the leader obtains a non-transferable payoff from holding office (ego rents, prestige, status, power, etc.) worth $F$ and is also endowed with $U$ units of transferable patronage (graft, cash, resource revenues, public offices, bribes, etc.).\(^{15}\) The leader then decides how to allocate the available patronage across the elite. Thus, if $\tau \in [0, U]$ units of patronage are allocated to the insiders in some period, then the leader obtains a payoff of $F + U - \tau$ in that period. The extent to which the benefits of office are transferable is captured by

$$\psi \equiv \frac{U}{F + U}. \quad (1)$$

Insiders observe their allocated patronage and decide whether they wish to mount a coup. Exactly one of the insiders has the opportunity to mount a coup in any given period, and this is determined randomly after the patronage has been allocated. A coup requires that the allocated patronage is forgone and succeeds with probability $\gamma$. If successful, the coup instigator becomes leader in the following period and the current leader dies. If unsuccessful, the coup instigator dies.

If there is no coup, the leader can choose whether to hold an election. Following an election, the leader chooses whether he is going to respect the result. Since election results can be ignored, there is no downside to holding an election in the model. Thus, to simplify the exposition we suppose that elections are always held and focus instead on whether the results are respected. We can then interpret a situation in which leaders never respect election losses as being equivalent to elections not being held.

\(^{14}\)None of our results hinge upon either having only two members of the elite, nor on symmetry across members of the elite. We discuss the implications of relaxing these assumptions in section 3.4.

\(^{15}\)Patronage is a ubiquitous feature of weakly institutionalized polities. For instance, Bratton and Van de Walle (1994) write: “The distinctive institutional hallmark of African regimes is neopatrimonialism. In neopatrimonial regimes, the chief executive maintains authority through personal patronage, ...The essence of neopatrimonialism is the award by public officials of personal favors, both within the state (notably public sector jobs) and in society (for instance licenses, contracts and projects). ...it is the core feature of politics in Africa...”. Patronage, graft and the state’s wealth are all clearly of a transferrable form, but it is equally realistic that no small part of the motivation for leading a country comes in the form of status and the even more nebulous form of “power”. A voluminous literature exploring the psyche of dictators attests to this. For example, much has been made of the self-aggrandizing aspects of power which satisfy deep personal needs within a particular type of leader, see Padilla, Hogan and Kaiser (2007). Again, it is conceivable that some of this could be transferrable – leaders can appoint a “right hand man” with immense power. But the residual component of a leader’s power in a weakly politicized state is inherently non-transferrable – the leader always has the right to “un-appoint” the right hand man too. These residual decision rights are similar in nature to those discussed in the theory of incomplete contracting a la Grossman and Hart (1986). A non-trivial component of power, and hence a leader’s status, seems inextricably linked to actually being the leader.
Each member of the elite dies with probability $\delta$ at the end of the period for exogenous reasons. An elite that dies is replaced by another in the next period and the replacement occupies the same position (leader or insider).

To summarize, the basic timing within a period is as follows:

1. Leader allocates patronage
2. Insider observes allocation and decides whether to mount a coup
3. If no coup, then election results revealed and Leader decides whether to respect them
4. Successors assume the role of any agents that die

We deliberately set aside the possibility of revolutionary threats from citizens. The one and only role of citizens is to decide the election outcome. We further emphasize that citizens do not have redistributive motives for voting: consistent with repeated observation in weakly politicized settings, citizens correctly anticipate that leaders do not deliver pro-citizen policies. Thus, for the most part, voters are essentially indifferent between candidates. When this is the case the incumbent wins the election with probability $p \in [0, 1]$. This state of indifference is broken however if a leader refuses to respect an election loss (equivalently, refuses to hold an election) when he was not expected to do so in equilibrium. In this event, voters become more reluctant to vote for the recalcitrant leader in the future. For modelling simplicity, we assume that voters will never vote for the recalcitrant leader ever again. Whilst there are many potential foundations for this voting behavior, for concreteness we pursue one possibility below.

3.1.1 Voting Outcomes

Leaders are one of two types: regular or tyrant. Tyrants are behavioural types that are obsessed with maintaining power–specifically, they never respect election results. A leader's type is not observed by citizens but we allow the leader and insiders to observe each others' types. All agents start off as regular types but become a tyrant type (permanently) with probability $\epsilon \to 0$ when they assume the leadership position. Citizens prefer not to be ruled by a tyrant because there is a small chance that a tyrannical leader will adversely affect them. Formally, that with probability $\eta \to 0$ the type of a leader effects citizens' payoffs; and it does so adversely if the leader is a tyrant. We emphasize the assumption of a very low $\eta$ to illustrate that an arbitrarily small preference on the part of citizens is sufficient here.

Our setting can accommodate the case where some voters have strong preferences for candidates, for instance because of ethnic, religious, or regional affinities. If each group has an equally large devoted following, then we can simply interpret "voters" to mean those voters without affinities to candidates.

Nothing hinges on this extreme formulation–all of our arguments remain if a recalcitrant leader is able to eventually redeem themselves over time. The value of this specification is that it allows us to work with a very simple state space.

This, in itself, is of no direct consequence to citizens, as citizens do not value the outcome of elections per se. But it becomes so when they expect non-tyrannical types to respect election results. That is, when a leader's not respecting an election result indicates – with a high probability – that the leader must be a tyrant type. As shall be seen, a key distinction between democratic and autocratic outcomes will hinge on voters' perceptions regarding a leader's type following the violation of election results.

All of the results we shall report fully persist if we assume tyrants are even more costly, in expectation, to citizens. As
Two important points arise from this structure. First, if both the leader and non-leader have always taken the equilibrium response to election losses, then citizens consider them equally likely to rule as a tyrant type—i.e. the leader is a tyrant with probability $\epsilon$ and the non-leader would become a tyrant with probability $\epsilon$. Second, if a leader refuses to step down when they are expected to do so in equilibrium, then citizens believe them to be a tyrant. This remains true even if such a leader were to subsequently step down. As a result, such a leader becomes uncompetitive in future elections.

### 3.1.2 States and Markov Strategies

Our analysis focuses on Markov Perfect Equilibria (MPE), whereby strategies depend only on the payoff relevant state variable and prior actions taken within the period. There are two relevant states, denoted $\{\omega_p, \omega_0\}$, differentiated by the probability with which citizens elect the incumbent. State $\omega_p$ represents the situation in which citizens are indifferent between the leader and non-leader. In this state the incumbent is re-elected with probability $p \in [0, 1]$. State $\omega_0$ represents the situation in which citizens are reluctant to vote for the incumbent because of the violation of an election result in the past. In this state the incumbent is elected with probability zero.

Transitions between these states work as follows. If regular leaders do not respect elections in state $\omega_p$, voter beliefs are unaffected when a leader refuses to step down in state $\omega_p$ and the economy thus remains in state $\omega_p$. On the other hand, if regular leaders do respect election outcomes in state $\omega_p$, refusing to step down following an election loss leads citizens to believe that the leader is a tyrant and the state transitions to $\omega_0$. Since it would never be optimal for the leader to voluntarily step down in this state, the leader will remain more likely than

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20If regular leaders always respect election losses in equilibrium, then we would never observe a leader that respects an election loss after having previously not respected an election loss on the equilibrium path. As such, citizen beliefs are not pinned down in this event. They would be pinned down in the manner described if, for example, election losers were forced to step down with a positive but arbitrarily small probability. In any case, all that we require is that such a leader does not fully redeem themselves by respecting an election.

21We consider equilibria with non-Markov strategies in section 4 below.

22This is shown formally in the appendix, but the intuition is as follows. If the leader stepped down, then they are more likely than the new incumbent to be a tyrant (and since $\eta \to 0$ we can ignore the possibility that the new incumbent reveals themselves to be a tyrant by taking the exploitative act). Since the new leader continues to win elections, there is no opportunity for them to violate an election loss and therefore their popularity (and that of their replacements) relative to the non-leader persists. Thus, if a perceived tyrant steps down, they will become a non-leader that will never be elected. This means that such a non-leader will be held to their expected value of mounting a coup. But even if the coup succeeds they only get the discounted value of being a leader in the $\omega_0$ state. In short, stepping down in state $\omega_0$ represents a strictly costly way to achieve what one could get by not stepping down in state a coup.
the challenger to be a tyrant. The economy thus remains in state \( \omega_0 \) until the leader dies—either naturally or via a coup—at which point citizen indifference re-emerges and the state transitions back to \( \omega_p \).

A Markov strategy for the leader maps the state \( \omega \in \{\omega_p, \omega_0\} \) into a patronage allocation and a probability of respecting an election loss. The strategy of an insider maps the state \( \omega \) into a function that indicates a coup probability for each potential amount of offered patronage transfer. We provide the full definition of Markov Perfect Equilibrium in the appendix, but opt to present more useful specialized definitions in the text that follows. Specifically, we consider the two natural classes of equilibria. The first is Autocratic equilibria, whereby leaders never respect election losses (equivalently, never hold elections), and the second is Democratic equilibria, whereby leaders always respect election results. These are considered in turn.

### 3.2 Autocratic Equilibrium

We begin by analysing equilibrium outcomes that arise when elections are ignored (equivalently, never held). Such equilibria, which we call autocratic equilibria, feature leaders that never share power with insiders. Despite this, autocratic leaders need not face coup attempts in equilibrium since they are able to share patronage with insiders. Since coups are costly, insiders can be dissuaded from holding them if they are offered enough of a transfer. Whilst one could imagine a leader preferring to face coups over making the transfers required to dissuade them, we shall demonstrate that this can never be the case—any political violence in equilibrium necessarily reflects insufficient patronage. We show how a generically unique autocratic equilibrium always exists, and depending on the availability of patronage can either never have coups (a secure autocracy), occasionally have coups (a weakly insecure autocracy), or always have coups (a strongly insecure autocracy). We also show that, unlike democracy, an unwillingness to share power is always self-enforcing: it is never optimal to hand over the leadership today if no-one is expected to hand over the leadership in the future.

#### 3.2.1 Equilibrium Conditions

If leaders never respect election losses, then voters’ beliefs about a leader’s type are not affected by a refusal to step down. As such, the economy only exists in a single state, \( \omega_p \). Equilibrium strategies reduce to a patronage transfer level, \( \tau_A \), and a coup probability function, \( c_A(\tau) \).

Let \( V^L_A \) be the value of starting a period as leader and \( V^N_A \) be the value of starting a period as the insider. The leader is optimizing in his transfer choice if

\[
\tau_A \in \arg \max_{\tau \in [0,U]} \left\{ F + U - \tau + (1 - c_A(\tau) \cdot \gamma) \cdot (1 - \delta) \cdot V^L_A \right\}
\]

(2)

and the insider is optimizing at each possible transfer if

\[
c_A(\tau) \in \arg \max_{c \in [0,1]} \left\{ c \cdot [\gamma \cdot (1 - \delta) \cdot V^L_A] + (1 - c) \cdot [\tau + (1 - \delta) \cdot V^N_A] \right\}
\]

(3)
for all $\tau \geq 0$. Given equilibrium outcomes, $\tau_A$ and $c_A = c_A(\tau_A)$, the value functions satisfy

$$ V_L^L = F + U - \tau_A + (1 - c_A \cdot \gamma) \cdot (1 - \delta) \cdot V_L^L $$

$$ V_L^N = c_A \cdot [\gamma \cdot (1 - \delta) \cdot V_L^L] + (1 - c_A) \cdot [\tau_A + (1 - \delta) \cdot V_N^N]. $$

In order for the leader to optimally ignore election results—i.e. in order for autocracy to be self-enforcing—it must be that

$$ V_L^L \geq V_L^N. $$

The strategies $\tau_A$ and $c_A(\tau)$ form an **autocratic equilibrium** if conditions (2)-(6) are satisfied. An autocratic equilibrium is said to be **secure** if $c_A = 0$, is said to be **strongly insecure** if $c_A = 1$, and said to be **weakly insecure** if $c_A \in (0, 1)$.

### 3.2.2 Analysis

Working backwards within a period, we first need to determine which transfers will dissuade insiders from mounting a coup given that they correctly anticipate that the leader will not hold/respect an election. From (3) it is clear that dissuading insiders from mounting coups requires that they are paid a critical transfer level. Denote this critical level $\hat{\tau}_A$ and note that $\hat{\tau}_A > 0$.\(^{23}\) Given this, the problem facing the leader is whether to pay $\hat{\tau}_A$ and enjoy reprieve from coups or to instead pay zero and face coups. Once this optimal decision is determined we need to verify that it is indeed optimal for leaders to ignore elections.

**Lemma 1.** Any autocratic equilibrium displays the following features.

1. **Coup are avoided whenever it is strictly feasible to do so:** $\hat{\tau}_A < U \Rightarrow \tau_A = \hat{\tau}_A$.
2. **Autocracy is always self-enforcing:** conditions (2)-(5) imply condition (6)

The intuition for the first part arises from the fact that coups are surplus destroying—either the leader or challenger dies with probability one—so avoiding them raises the surplus of the game played by insiders and leader. This efficiency gain, which can always claimed by the leader through his discretionary allocations of $\tau_A$ when $\hat{\tau}_A < U$, ensures that coups are avoided along the equilibrium path in such cases.

The requirement that autocracy is self-enforcing seems to be threatened by the observation that the leadership is unattractive when subject to frequent coup attempts and/or high patronage demands whilst being an insider is attractive to the extent that they are able to use the threat of coups to extract patronage transfers. The second part indicates that such a threat never materializes. The intuition follows from noting that a leader becomes an insider by stepping down. Since insiders can mount a coup, they can ensure themselves at least the expected value of coups. But in autocracy, this is also the most that they can achieve, since leaders do not relinquish power. But this is strictly less than the value of being the leader, partly because coups are not always successful.

Given the general features of autocratic equilibrium highlighted by Lemma 1, the nature of such equilibria will clearly depend upon whether patronage is sufficiently transferable to

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\(^{23}\)The intuition is straightforward—if instead $\hat{\tau}_A \leq 0$, then the insider would be unwilling to mount a coup even if they were not transferred anything. But if they get no transfers, then there is nothing to lose by mounting a coup.
make the required payments to insiders. In order to help state the following proposition, recall that the transferability of patronage is denoted $\psi \equiv \frac{U}{(U + F)}$, and define two critical values $\mu_1 \equiv \frac{\delta \gamma (1-\delta)}{\sigma + \gamma (1-\delta)}$ and $\mu_2 \equiv \frac{\gamma (1-\delta)}{\sigma + \gamma (1-\delta)}$, noting that $0 < \mu_1 < \mu_2 < 1$.

**Proposition 1.** An Autocratic equilibrium always exists and is generically unique. Specifically:

- A secure Autocratic equilibrium exists if and only if $\psi \geq \mu_2$,
- A weakly insecure Autocratic equilibrium exists if and only if $\psi \in (\mu_1, \mu_2)$, and
- A strongly insecure Autocratic equilibrium exists if and only if $\psi \leq \mu_1$.

When patronage is sufficiently abundant, $\psi \geq \mu_2$, leaders can pay insiders enough to fully dissuade them from holding a coup when anticipating becoming a secure autocrat. When patronage falls in the middle region, $\psi \in (\mu_1, \mu_2)$, there is not enough to dissuade insiders from holding a coup when anticipating becoming a secure autocrat, yet does there is enough patronage to dissuade them when anticipating becoming a strongly insecure autocrat. In this region, all available patronage is transferred and insiders hold coups with a probability that makes them indifferent between accepting the transfer and mounting a coup anticipating themselves becoming a weakly insecure autocrat. As patronage is lowered within this region, so too is the transfer to insiders. This makes coups more attractive and thus the probability of a coup rises as patronage falls. When low enough, i.e., $\psi$ at or below $\mu_2$, the probability of a coup becomes so great that leaders prefer to keep the transfer and face coups with probability one. Leaders are therefore resigned to facing coups each period when patronage is sufficiently scarce.

This proposition links the stability of autocracies to the existence of a steady stream of patronage rents; a theme already well reflected in the study of autocracies. For example, Van de Walle (1994):

“Cameroon’s “patrimonial orientation” was due to its political leaders’ management of oil wealth and that this wealth, along with foreign aid, allowed the authoritarian regime to endure.”

Fjelde (2009):

“The conversion of public funds into private payoffs has prolonged poverty and bred economic inequality in many oil-wealthy states, but it has also helped foster powerful alliances with a stake in the continuation of the prevailing rule (Smith, 2004). Countries such as Gabon, Libya and Saudi Arabia illustrate how oil-based rent-seeking can strengthen regimes, by exiting their clientelist networks and thus placating restive groups.”

And:

“Oil-rich Gabon provides another illustration of how oil wealth and institutionalized corruption have converged to produce relatively high political stability, ...the political stability of Gabon has relied crucially on the president’s (Bango) patronage networks. These have derived their strength from a careful ethnic balancing in the ethnically diverse country and a deliberate integration of powerful political opponents into the regime’s power base (Yates, 1996; Basedau & Lacher, 2006).” p.203
For much of the relevant parameter space, the marginal dollar of patronage is best used by an autocrat as a transfer to insiders to increase (or maintain) regime security rather than fully retained as consumption. The logic stems from part 1 of Lemma 1, where we showed that autocrats are willing to avoid coups whenever possible. Only strongly insecure autocrats, those for whom $\psi < \mu_1$, would retain marginal increases in patronage, as for them peace is unaffordable.

An autocratic equilibrium involves wasteful coups only if patronage is insufficient. This observation hints at the underlying value that the elites may find in minimalist democracy: the inability to avoid coups via patronage could possibly be overcome if insiders could instead be offered the possibility of future power via elections. We now turn to this issue.

### 3.3 Minimalist Democracy Equilibrium

A minimalist democracy equilibrium has two key features. The first is use of, and respect for, elections, and the second is that democratic leaders do not have their rule truncated by coups. Democratic equilibria involve peaceful power transfers among the elite. Coups are dissuaded by the promise of legitimately obtaining power via elections (as well as patronage transfers in some cases). It will be seen that the principal reason leaders respect election losses is that because failing to do so will render them uncompetitive in future elections. This condemns them to rule as a tyrant (a type of ruler who will never be approved by the public), and minimalist democracy depends on ruling as a tyrant being sufficiently unattractive, which happens when insiders are especially motivated to mount coups against tyrants.

#### 3.3.1 Equilibrium Conditions

Since leaders respect election losses in this equilibrium, a failure to do so leads voters to update their beliefs about a leader’s type. The leader is perceived to be a tyrant and is never elected again. Thus, both states $\omega_p$ and $\omega_0$ need to be considered. In state $\omega_p$, voters perceive candidates to be equally attractive since both candidates have respected elections in the past. We shall refer to $\omega_p$ as the “democratic” state in this equilibrium. In state $\omega_0$ the leader has refused to respect an election loss in the past and is therefore perceived to be a tyrant by voters. We shall refer to $\omega_0$ as the “tyranny” state in this equilibrium.

The democratic state persists if the leader wins the election, loses the election and steps down, or dies. If the leader loses election and stays, the state transitions to the tyranny state. The tyranny state persists as long as the leader stays in power, and transitions back to the democratic state if he dies or is deposed.

Equilibrium strategies boil down to a patronage transfer level and a coup probability function for each of the two states: $\{\tau_p, c_p(\tau)\}, \{\tau_T, c_T(\tau)\}$. We first establish the optimality of behavior at each decision point. Let $V_p^L$ and $V_T^L$ be the values of starting a period as the leader in the democratic and tyranny states respectively, and similarly let $V_p^N$ and $V_T^N$ be the values of starting a period as an insider in each of the states.

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$^2$Note that $\omega_p$ has no such interpretation in the autocratic equilibrium.
In the democratic state, the leader is optimizing in their transfer choice if
\[
\tau_D \in \arg \max_{\tau \in [0,U]} \{ F + U - \tau + (1 - c_D(\tau) \cdot \gamma) \cdot (1 - \delta) \cdot \langle p \cdot V^L_D + (1 - p) \cdot V^N_D \rangle \} \tag{7}
\]
and the insider is optimizing at each possible transfer if
\[
c_D(\tau) \in \arg \max_{c \in [0,1]} \{ c \cdot \langle (1 - \delta) \cdot V^L_D \rangle + (1 - c) \cdot \langle (1 - \delta) \cdot (p \cdot V^N_D + (1 - p) \cdot V^L_D) \rangle \} \tag{8}
\]
In the tyranny state, the leader is optimizing in their transfer choice if
\[
\tau_T \in \arg \max_{\tau \in [0,U]} \{ F + U - \tau + (1 - c_T(\tau) \cdot \gamma) \cdot (1 - \delta) \cdot V^L_T \} \tag{9}
\]
and the insider is optimizing at each possible transfer if
\[
c_T(\tau) \in \arg \max_{c \in [0,1]} \{ c \cdot \langle (1 - \delta) \cdot V^L_T \rangle + (1 - c) \cdot \langle (1 - \delta) \cdot (p \cdot V^N_T + (1 - p) \cdot V^L_T) \rangle \} \tag{10}
\]
Given equilibrium outcomes, \( \tau_D, \tau_T \) and \( c_T \equiv c(\tau_T) \), the value functions satisfy
\[
V^L_D = F + U - \tau_D + (1 - \delta) \cdot (p \cdot V^L_D + (1 - p) \cdot V^N_D) \tag{11}
\]
\[
V^N_D = \tau_D + (1 - \delta) \cdot (p \cdot V^N_D + (1 - p) \cdot V^L_D) \tag{12}
\]
and
\[
V^L_T = F + U - \tau_T + (1 - c_T \cdot \gamma) \cdot (1 - \delta) \cdot V^L_T \tag{13}
\]
\[
V^N_T = c_T \cdot (1 - \delta) \cdot V^L_T + (1 - c_T) \cdot \langle \tau_T + (1 - \delta) \cdot (p \cdot V^N_T + (1 - p) \cdot V^L_T) \rangle \tag{14}
\]
In the democratic phase, equations (11) and (12), value functions reflect that leaders do not face coups, so only transition out of leadership via election losses, \( p \). Insiders face the reciprocal probability of moving to power. Tyrannic value functions, equations (13) and (14), are similar to the autocracy case we studied previously. A difference is that, in case of leader death via either coup success or exogenous causes, since democracy is a preferred governance mode, the replacement leader will govern democratically and value functions reflect a transition back to the democratic phase.

We must verify that two key conditions are satisfied. First, we must verify that democracy is peaceful—i.e. that there must be no coups in the democracy state:
\[
\tau_D + (1 - \delta) \cdot (p \cdot V^N_D + (1 - p) \cdot V^L_D) \geq \gamma \cdot (1 - \delta) \cdot V^L_D. \tag{15}
\]
Second, we must verify that it is optimal for a leader to optimally step down following an election defeat. That is, for democracy to be self-enforcing, the leader in the democracy state must prefer being an insider in democracy to being a leader in the tyranny state:25
\[
V^N_D \geq V^L_T. \tag{16}
\]

The strategies \( \{\tau_D, c_D(\tau)\}, \{\tau_T, c_T(\tau)\} \) constitute a minimalist democracy equilibrium if (7)-(16) are satisfied.

We proceed by first deriving the parameters under which the ‘no-coups’ condition will hold in a minimalist democracy equilibrium. We then refine this set of parameters to include only those for which the ‘self enforcing’ condition will also hold. This refined set characterizes the conditions under which a minimalist democracy exists.

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25 To be complete, we also need to verify that a leader in the democratic state prefers to hold an election than to act as a leader in the tyranny state. That is, that \( V^L_D \geq V^L_T \). But this is implied by the self-enforcing condition once we verify that \( V^N_D \geq V^N_T \). This is formally proved in Result 2 in the appendix.
3.3.2 Analysis: No coups

It is clear from (8) that the insider in the democratic state requires a critical transfer in order to dissuade them from mounting a coup. Denote this critical transfer level $\hat{\tau}_D$. Note that the required transfers are generally lower than an autocrat would have to pay as the leader in a democracy is also allowing insiders a chance to power through elections. Indeed, we shall see that the required transfer is sometimes negative (so that coups are avoided even if no transfers are made). The ‘no coups’ condition will definitely be violated if $\hat{\tau}_D > U$ (i.e. whenever the required transfer is infeasible). The following result indicates that democratic leaders will avoid coups in all other cases.

Lemma 2. Democratic leaders find it optimal to avoid coups whenever it is feasible. That is, if $\hat{\tau}_D \leq 0$ then setting $\tau_D = 0$ is optimal, and if $\hat{\tau}_D \in (0, U]$ then setting $\tau_D = \hat{\tau}_D$ is optimal.

In other words, if the ‘no coups’ condition violated it is never because of an optimal choice on the part of a democratic leader. The logic for why democratic leaders will never choose to face coups is similar to the coup dissuading choice of an autocrat in the previous section. Coups destroy surplus, so if feasible to dissuade them by transfers the leader is strictly better off by doing so.

Lemma 2 implies the ‘no-coup’ condition is satisfied if and only if parameters are such that required transfers are feasible. The conditions for this are characterized in the following lemma. To aid in the expression of the result, define $p^* \equiv \frac{1-\gamma}{1-\gamma(1-\delta)}$ and $f(p) \equiv \frac{1-\delta\gamma(\gamma-p(1-\delta)+1-p)}{\delta(1+p(1-\delta))}$.

Lemma 3. The ‘no coups’ condition, (15), is satisfied if $p$ is sufficiently low or if $\psi$ is sufficiently high. Specifically, it is satisfied with zero transfers if and only if $p \leq p^*$, and is satisfied with positive transfers if and only if $p > p^*$ and $\psi \geq f(p)$.

Democracy is peaceful under the conditions established in Lemma 3 and illustrated in figure 13. There are two (disjoint) sets of parameters, $P_1$ and $P_2$, such that peaceful transfers are achieved with zero transfers in $P_1$ and with positive transfers in $P_2$. To explain the shape of $P_1$, suppose that democratic equilibrium involved zero transfers so that the leader gets all the benefits from office. In order to dissuade a coup, it must be that insiders anticipate becoming the leader with sufficiently high probability (i.e. $p \leq p^*$). The extent to which the benefits from office are transferable is immaterial since no transfers are made. In order to explain the shape of $P_2$, suppose instead that the insider does not have a high enough chance of winning an election (i.e. $p > p^*$) so that a positive transfer is required to dissuade a coup. In order for the required transfer to be feasible it must be that patronage is sufficiently abundant ($\psi \geq f(p)$). Furthermore, an insider requires a greater transfer to avoid a coup—and thus feasibility requires greater levels of patronage—as their electoral prospects worsen (i.e. $f$ is increasing in $p$).

The fact that $P_1$ and $P_2$ are disjoint rules out the possibility that a democratic equilibrium with zero transfers coexists alongside one with positive transfers. Result 3 in the appendix establishes the uniqueness of transfers in democratic equilibrium in general.

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Formally, $P_1 \equiv \{p, \delta, \gamma, U, F \mid p \leq p^*\}$ and $P_2 \equiv \{p, \delta, \gamma, U, F \mid p > p^*, \psi \geq f(p)\}$. 

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3.3.3 Analysis: Respecting Elections

We now turn to the condition that election losers optimally step down. This condition compares the value of being an insider in the democratic state, $V_N^D$, with that of being a leader in the tyranny state, $V_L^T$. The value of $V_N^D$ has been pinned down by the above analysis,\(^{27}\) so we now turn to an analysis of play in the tyranny state.

The tyranny state is triggered when the leader refuses to step down following an election. Citizens perceive the leader to be a tyrant with a greater probability than a challenger and therefore the leader is sure to lose any future election. There is no benefit from stepping down so he will therefore remain in office until deposed via coup or death.

The tyrant leader is similar to the autocrat except that they face insiders who anticipate becoming a democratic leader following a successful coup (as opposed to becoming an autocrat). As with an autocrat, a tyrant may be secure (face coups with zero probability) or insecure (face coups with a positive probability). In determining whether a tyrant is secure, we note from (10) that the insider in the tyranny state must be transferred a critical amount in order to be dissuaded from coups. Denote this $\hat{\tau}_T$. This quantity is important for determining whether democracy is self-enforcing since it governs how costly it is to lead in the tyranny state. The following result indicates that secure tyranny is never costly enough a prospect to convince election losers to step down.

**Lemma 4.** Leaders respect elections only if leaders in the tyranny state are insecure.

In other words, democracies can be self-enforcing only when a leader violating democratic rules is forced to rule as a tyrant that faces perpetual existential threats. Intuitively, if peace is available to a tyrant leader then the total surplus available to all players in the game is the same in both the democratic and tyranny states. Under tyranny, the leader transfers just enough of this surplus to insiders to buy peace, and thus makes them indifferent to undertaking coups. Necessarily then under democracy either the leader transfers $\tau_D > 0$ leaving insiders indifferent to coups, or $\tau_D = 0$. In the latter case, the possibility of winning power through elections is sufficient to motivate insider loyalty. But then insiders strictly prefer loyalty over taking a coup, implying that their share of the surplus exceeds that which they would obtain under tyranny – where leader transfers make them just indifferent to undertaking coups. Necessarily then, leaders share more of the (same total) surplus with insiders in democracy than they do with insiders under secure tyranny, implying that tyrannical rule must be preferred. Alternatively, the leader makes a positive transfer to insiders so that they are just indifferent to taking a coup under tyranny. But this implies that the leader’s share of the total surplus is as high under democracy as it would be under tyranny. When that is the case a leader would never voluntarily step down from leadership, as staying on and ruling as a tyrant is just as good. In either case, democracy cannot be self-enforcing.

We show in the appendix (Lemma 6) that leaders in the tyranny state, as in the autocratic equilibrium, will optimally avoid coups whenever strictly feasible. As such democracy is self-enforcing only if peace is infeasible for leaders in the tyranny state. The following result uses this to further refine the set of parameters (beyond $P \equiv P_1 \cup P_2$ from Lemma 3) for which a

\(^{27}\)Specifically, the value of $\{V_L^T, V_N^D\}$ are the solutions to (11) and (12) where $\tau_D = 0$ if parameters are in $P_1$ and $\tau_D = \hat{\tau}_T$ (as defined in (33)) if parameters are in $P_2$. 

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minimalist democracy can exist.

**Lemma 5.** A tyrant is insecure—and thus the self-enforcing condition can hold—only if $p$ is sufficiently large or $\psi$ is sufficiently small. Specifically, only if

- $\psi \leq g(p) \equiv \frac{1−\delta+2(1−\delta)(1−p)(1−\gamma)(1−p)(1−\delta)}{2−2(1−\delta)p}$ if parameters are in $P_1$, or
- $\psi \leq \mu_2$ if parameters are in $P_2$.

Lemma 5 identifies a tighter set of necessary conditions for the existence of democratic equilibrium, as illustrated in figure 14; where democracy is self-enforcing only if parameters are in $S_1$ or $S_2$ (which are subsets of $P_1$ and $P_2$). A democratic equilibrium with zero transfers exists only if parameters are in $S_1$ and a democratic equilibrium with positive transfers exists only if parameters are in $S_2$. First consider $S_1$, where the democratic equilibrium involves zero transfers. A larger $p$ makes elections more biased toward incumbents, and since transfers are zero, necessarily, leaders are better off. But this gives insiders under tyranny a greater incentive to mount a coup, making tyranny even less attractive, in the sense that a greater transfer is required to dissuade a coup. Thus the upper boundary of $S_1$ is upward sloping. On the other hand, in $S_2$, democratic equilibrium necessarily involves positive transfers. A larger $p$ makes elections more incumbent friendly, inducing insiders to more greatly prefer coups and thus raising the equilibrium transfers required. But this implies the net effect on payoffs is unaffected. Thus, the payoff to being a democratic leader is unchanging in $p$, incentives for insiders to mount a coup against a tyrant are also unchanged, so the security of tyranny is unaffected, and therefore the upper boundary of $S_2$ is flat.

Importantly, the conditions that democracy requires in order to be self-enforcing are of the opposite nature to those democracy requires to be peaceful: patronage must be sufficiently low or elections must be sufficiently favorable to the incumbent. As is clear from the above, tyrannical rule is insecure with low levels of patronage. This makes it an unattractive choice for a leader, so he respects democratic rules. But this is also the reason why $p$ cannot be too low. Insiders who depose tyrants via coups rule as democrats, so that when $p$ is low, the attractiveness of coups is also low, making tyrannical rule more secure.

This result is opposite to that of Fearon (2011) who also studied a similar credibility of elections problem. Fearon considered the incentives for members of the public to undertake a rebellion to unseat a leader who had overstayed his electoral mandate. Elections helped in coordinating citizens in their act of rebellion and hence helped in sustaining equilibria where elections would become self-enforcing. In his framework they are more likely to be self-enforcing the lower is $p$ (i.e., the analogue of $p$ in his model). The reasoning is in line with the original (informal) argument along these lines by Przeworski (1991). Incumbents will step down in the event of losing elections only if $p$ is sufficiently low because the probability of the incumbent coming back in to office is greater if $p$ is low (in the limit, with $p$ approaching 1, stepping down means remaining out of power indefinitely). The continuation value of leaving thus falls with $p$, and if $p$ is high enough, makes the incumbent willing to stay after a loss even though it means facing a rebellion. The difference in results arises because it is the threat of rebellion that disciplines leaders to step aside. This threat, unlike the coups that we study, is exogenous to the political process, in the sense that the magnitude of the threat, i.e., the

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28Formally, $S_1 \equiv \{p, \delta, \gamma, U, F \mid \psi \leq g(p)\} \cap P_1$ and $S_2 \equiv \{p, \delta, \gamma, U, F \mid \psi \leq \mu_2\} \cap P_2$. 

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willingness of the public to rebel, is independent of the parameters of the political process. In our set-up, the leader is threatened by endogenous coups, the returns to which are themselves dependent on the parameters of the political system. Since, for the reasons discussed above, the value of becoming leader via a coup is increasing in \( p \), \( p \) must then be sufficiently great to make elections self-enforcing.

### 3.3.4 Existence of Democratic Equilibrium

We now turn to the question of existence of democratic equilibrium. So far we have that a democratic equilibrium exists only if parameters are in \( S_1 \) or \( S_2 \). But being insecure is, in general, not sufficient to ensure that elections are respected. For sufficiency, leaders must also prefer to step down upon election loss rather than leading as an insecure tyrant. Intuitively, this requires that coups have a sufficiently high probability of succeeding, i.e., \( \gamma \) is high relative to \( \delta \).

**Proposition 2.** If \( \gamma \geq \delta^{1/2}/(1 - \delta) \), then a democratic equilibrium exists if and only if tyrants are insecure (and there are no coups in the democratic state). That is, if and only if (i) \( p \leq p^* \) and \( \psi \leq g(p) \), or (ii) \( p > p^* \) and \( \psi \in [f(p), \mu_2] \). Furthermore, the equilibrium is generically unique. Specifically,

- if \( p \leq p^* \) and \( \psi < g(p) \), the equilibrium involves zero transfers in the democracy state, and zero transfers and coups with probability one in the tyranny state.
- if \( p > p^* \) and \( \psi \in [f(p), \mu_2] \), the equilibrium involves positive transfers in the democracy state, and zero transfers and coups with probability one in the tyranny state.

The restriction on \( \gamma \) simply ensures that being an insecure tyrant is worse than a transfer-receiving insider. Since insecure tyrants do not face elections their welfare is independent of \( p \). However insider welfare is non-increasing with \( p \). If the insider transfers are zero (\( p < p^* \)) a marginal increase in \( p \) extends the expected time to an election victory, strictly lowering welfare. For \( p > p^* \) transfers are designed by the leader to just dissuade coups. Higher \( p^* \)'s are thus offset by lower transfers making insiders' values flat in this region. Insider value is thus minimized (with respect to \( p \)) whenever insiders receive positive transfers. Provided the value of being an insecure tyrant is lower than this minimized value, leaders will choose to respect elections rather than stay on as tyrants.

With this condition met, the possibility of democracy depends both on the requirement that it is peaceful and that it is self-enforcing. Peace, or no-coups, places a lower bound on patronage/upper bound on \( p \) whereas the self-enforcing condition places an upper bound on patronage/lower bound on \( p \). Hence the marked contrast with preconditions in Fearon (2011) for this case. Note finally that the condition is not restrictive—e.g. it holds for any \( \gamma \) as long as agents are sufficiently concerned about the future (i.e. as long as \( \delta \) is low enough).

If \( \gamma \) is marginally lower than required for the above to hold, then insecure tyranny does not immediately ensure that democracy is self-enforcing. Nevertheless, democracy can still be so if the value of being an insider is greater (that is, for values of \( p < p^* \)). This implies that democracy must involve zero transfers in this case.
Proposition 3. If $\gamma < \delta^{1/2}/(1-\delta)$, then a democratic equilibrium exists if and only if $\psi \leq g(p)$ and $p$ is sufficiently small that

$$\frac{p}{1-p} \leq \gamma \left(\frac{1-\delta}{\delta}\right)^2 - \frac{1}{\delta}.$$ \hfill (17)

Such an equilibrium is generically unique, and involves zero transfers in the democratic state.

When this condition is met, democratic equilibrium is constrained only by the self-enforcing condition. Specifically, $p$ must be high enough that tyrants are insecure but low enough that insiders are sufficiently optimistic about returning to power in the future.

The problem a leader faces in pursuing a democratic strategy rests with the credibility of the leader’s claims to respect democracy, and the adequacy of promised electoral processes in appeasing the elite. These two propositions characterize the full parameter range in which these problems are solved. Credibility depends on the interaction between the patronage value of the state, and the nature of electoral processes in democracy. For low values of $p$ a democratic equilibrium will exist provided the patronage value of the state is not too high. For higher values of $p$ patronage helps keep peace in democracy. Since leaders enjoy large incumbency advantages and are removed by elections only rarely, insiders must receive sufficient transfers to eschew coup opportunities, but without sufficient patronage leaders will not be able to meet these transfers. It is still the case in this region though that patronage levels cannot become too large or autocracy will be secure, and hence chosen by leaders.

3.4 Discussion of Assumptions

The model presented above captures the logic that a powerful political elite can use elections in order to circumvent the coup threat arising from the imperfect transferability of office via inter-temporal power-sharing. Our main theoretical results are concerned with characterizing when such power-sharing arrangements are supported in equilibrium, and highlights the need for leaders to be sufficiently sheltered from coup threats that power is not seized in equilibrium, yet sufficiently exposed to them that they fear violating an election. These qualitative features and results remain if (i) we allow there to be more than two elites at a given date, and (ii) we introduce asymmetries across members of the elite.

Suppose that there were $N > 2$ members of the elite, one leader and $N - 1$ insiders, and that the opportunity to mount a coup arises for one randomly chosen insider each period. Coup threats are heightened relative to the $N = 2$ case. For instance, the insider needs a larger transfer from a secure autocrat in order to dissuade a coup since the insider will have to wait longer on average for another chance to threaten a coup. If the leader did not observe which elite was the one with the coup opportunity, then they would have to pay all of them enough if a coup is to be avoided. In either case the underlying motivation for establishing a minimalist democracy—the inability to make required transfers—is only intensified when there are more members of the elite to satisfy. However, there is no unambiguous effect of $N$ on the capacity to support minimalist democracy; the heightened coup threat makes the ‘no coup’ condition more difficult to satisfy but the ‘self-enforcing’ condition easier to satisfy.

The analysis would be needlessly complicated by introducing asymmetry across the elite, for instance by allowing different values of $\gamma$ or $p$. The reason is that we could not rely on
symmetric strategies and (even if we remained with Markov strategies) would therefore have to consider a range of uninteresting special cases. For instance, having a minimalist democracy being supported by only one of the two elites paying the other when leader. Nevertheless, the implications of such asymmetries are intuitive. For instance if elite $i \in \{1, 2\}$ (and their replacements) has a coup success probability of $\gamma_i$ where $\gamma_1 > \gamma_2$, then the ‘no coup’ condition is more difficult to satisfy when elite 2 is in power (since elite 1 requires a greater payment) and the ‘self enforcing’ condition is more difficult to satisfy when elite 1 is in power (since elite 2 can be bought off, in the tyranny phase, more easily). Alternatively, we could have the elite differ with respect to their electoral chances by supposing that elite $i \in \{1, 2\}$ is re-elected as incumbent with probability $p_i$, with $p_1 > p_2$. This would clearly have no effect in the autocratic equilibrium. However, elite 1 holds a greater value associated with being the leader in democracy (since their expected tenure is longer), and is therefore more willing to mount a coup. As such the ‘no coup’ condition is more difficult to satisfy when elite 2 is in power whereas the ‘self enforcing’ condition is more difficult to satisfy when elite 1 is in power.

4 The Role of Elections and Non-Markov Equilibria

Our theory of minimalist democracy demonstrates how peaceful power-sharing among elites can be achieved via the use of elections. But can such arrangements be achieved without elections, especially if we expand our scope to consider non-Markov equilibria? If so, what advantages do elections have over the alternatives? We turn to these questions in this section.

In the equilibria analyzed above, the voters play the role of a randomization device that determines when power is to shift hands. However, their role is more than this owing to their aversion to voting for a leader that has ignored election results in the past. To see the importance of this role, suppose that we ignored voters altogether but instead endowed the elites with a randomization device that dictates when power is to be handed over. This device could be made as similar as we like to that of elections studied above, i.e., it can be set to generate a binary signal with the leader being able to “stay” with probability $p$ or “leave” with $1-p$. Supporting peaceful power-sharing in this setting requires non-Markov strategies, yet the strategic environment of our democratic equilibrium can be replicated here. Simply have agents play the same strategies as described in the democratic equilibrium except that a leader’s violation of the power sharing rule triggers a ‘punishment phase’ in which insiders hold coups until the leader is replaced. That is, a violating leader is forced to rule as a tyrant not because voters leave no other option but, rather, because their observed violation facilitates a coordinated shift toward punitive actions by the other insiders.

A problem with power-sharing constructed this way, however, is that it is supported by threats to pursue a punishment path that is Pareto dominated; i.e. such an equilibrium without elections is not renegotiation proof (Farrell and Maskin (1989), Bernheim and Ray (1989)). Specifically, both the leader and insider prefer, at least one strictly, to return to the equilibria.

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29Since the outcome of the randomization device is not payoff relevant, Markov strategies are not rich enough to allow punishments following a leader’s refusal to step down when required by the randomization device. As such, power sharing would not be possible in Markov strategies. This is not true in the main model above, where there are voters who are unwilling to re-elect election violators. Such an unwillingness is both rational and payoff relevant.
rium path following a leader’s refusal to step down. Naturally the leader prefers to return to the equilibrium path: the fact that the leader respects the power-sharing rule in equilibrium implies that they would in fact even weakly prefer to return to the equilibrium path as an insider, and therefore strictly prefer to return as the leader. Perhaps less obviously, the insider also prefers to return to the equilibrium path. This follows by observing that all coups, whether aimed at disciplining the leader or at an opportunistic seizure of power, are treated the same in equilibrium—a successful coup allows the new leader to rule ‘with a clean slate’. The value of mounting a coup on the punishment path is therefore the same as the value of mounting a coup off the equilibrium path. But since there are no coups against non-tyrants in equilibrium, the latter value is no greater than the value of being an insider on the equilibrium path. Thus an insider would always prefer to return to the equilibrium path over continuing with the punishment so that both players would willingly renegotiate back to equilibrium play rather than pursue punishment strategies.

In contrast, issues of renegotiation during the punishment phase are circumvented by introducing elections. Voters effectively strip a violating leader of future access to the power-sharing technology. That is, renegotiating back to the equilibrium path is not an option for a leader that has violated an election outcome. In this light, elections are more than a simple randomization device – instead, they are a randomization device that has the important property of becoming biased against those that have violated its directive in the past.

This rationale for use of elections—that they bolster the credibility of punishments supporting power-sharing agreements—complements existing rationales that stress other features. Fearon (2011) emphasizes how the regularity of elections helps citizens impose their will on leaders by providing them with a means to coordinate a rebellion. Coordination is not an issue for us—citizens have no power over the elite and coups are mounted unilaterally by insiders. Przeworski (1999) instead emphasizes the role of “ballots vs. bullets”: the idea that elections help gauge the relative strength of competing factions and thus help avoid bloodshed by providing a reasonable prediction of the result of violent conflict. This avenue does not operate in our model either since there is no uncertainty over the consequences of conflict (i.e. coups).  

4.1 Alternative Strategies to Support Power-Sharing

The previous section has shown how elections allow for power-sharing via the described strategies even though these would otherwise fail to be renegotiation-proof. Here we explore the extent to which power-sharing can be supported without elections using other strategies that are renegotiation-proof. Specifically, we are interested in “power-sharing equilibria”—i.e. equilibria of the repeated game played by the elite in which leadership changes hands periodically in a peaceful manner. These equilibria are distinguished from our Minimalist Democracy Equilibrium since the latter necessarily involves voters.

30Przeworski (1999) also raises, but dismisses, the possibility that elections compel citizens to accept the decisions of leaders because voting imposes an obligation to respect the outcome. Similarly the elite in our model have no need to seek such an obligation—their hold on power is not directly tied to their perceived legitimacy. However, it is indirectly, since an equilibrium outcome is the continued ability to use elections depends upon respecting them in the past. Without this ability, leaders would face constant threats from excluded insiders.
We begin by identifying an attractive property of our minimalist democracy equilibrium, related to the treatment of coups, and then go on to show it is necessarily absent in any power-sharing equilibrium that is renegotiation-proof.

In considering the minimalist democracy equilibrium, coups can be classified into two categories. First, an *opportunistic coup* is one mounted against a player that has never deviated from their equilibrium strategies (and is not a behavioural tyrant type). This sort of coup is motivated by the prospect of seizing the leadership and does not arise on the equilibrium path. Second, a *disciplining coup* is one mounted against a player that has either deviated in the past (e.g. by not holding an election, by holding a rigged election, by not respecting the election outcome, by not making the required transfer, or by undertaking an opportunistic coup) or has become a behavioural tyrant type. Such coups do arise on the equilibrium path and must also arise in the (off-equilibrium) sub-games following players’ deviations.

In a minimalist democracy equilibrium both coups are treated identically, but we will argue here that power-sharing equilibria necessitate differential treatment – disciplining coups are encouraged and opportunistic coups must be discouraged. Before demonstrating this formally, first note the heavy informational assumptions required for coups to be differently treated. Since opportunistic coups are not supposed to arise in equilibrium, future players – unless they know the nature of the coup with certainty – will rationally interpret any coup as a disciplining coup mounted against a behavioural tyrant. To disguise the true reason, the instigator of an opportunistic coup could thus always maintain that they did not receive the required transfer, or that the election was rigged, or perhaps even that the current leader seized power via an opportunistic coup. In short, it seems very easy in reality to disguise opportunistic coups as disciplining coups without intimate knowledge of current and past events and circumstances. If we take the possibility seriously that the motivation for coups is unlikely to be public knowledge, then the fact that the minimalist democracy equilibrium strategies treat opportunistic coups and disciplining coups the same (i.e. they have the same continuation value) is a highly desirable feature.

Is it possible to construct power sharing equilibria that share this feature? Define equilibrium strategies as having *coup symmetry* if there exists at least one opportunistic coup on the equilibrium path and one disciplining coup (not necessarily on the equilibrium path) such that the continuation value of the opportunistic coup is at least as large as that of the disciplining coup. This property is weaker than requiring all coups be treated equally (as they are in a minimalist democracy equilibrium) as it allows opportunistic coups to have strictly lower continuation values than disciplining coups. It requires only that the highest continuation value following an opportunistic coup on the equilibrium path is at least as great as the lowest continuation value following any disciplining coup. The following result shows that even this weak requirement is too stringent a demand on power-sharing equilibria.

**Proposition 4.** There does not exist a power-sharing equilibrium that is renegotiation-proof and has coup symmetry.

Rewarding disciplining coups so that renegotiation back to the equilibrium path is not chosen by an insider must necessarily clash with dissuading insiders from opportunistic coups, unless these differing types of coups lead to different continuation values.

Proposition 4 ensures that any renegotiation-proof power-sharing equilibrium features
all opportunistic coups having continuation values strictly lower than all disciplining coups. Thus, necessarily, power-sharing equilibria require current and future insiders to know the nature of any coup. Under the reasonable assumption that insiders do not know the true reason for a coup, it is not possible to construct a power-sharing equilibrium (i.e., by using a non-electoral randomization device) that is also renegotiation-proof. We reiterate that this same assumption, applied to the minimalist democracy framework we have studied above, has no effect, since coups are treated identically by players irrespective of the reason for the coup.

4.1.1 Power-sharing equilibria when insiders can know the reasons for coups

It remains to be seen whether it is possible to construct renegotiation proof strategies when the reasons for coups are public knowledge. A promising possibility would seem to be the use of strategies that are similar to the minimal democracy equilibrium ones except that those instigating opportunistic coups are also subject to perpetual coups (insiders can still mount disciplining coups with impunity). To see how this could be renegotiation-proof, classify a leader as “illegitimate” if they have ever violated the power-sharing rule, or came to power via a coup against a leader that had never violated the power-sharing rule, otherwise classify them as “legitimate”. There will tend to be a high value of being the leader and a low value of being an insider since the threat of launching an opportunistic coup is weakened by the fact that doing so would, at best, render the instigator an illegitimate leader. Being an illegitimate leader is unattractive since insiders can mount coups without fear of losing their legitimacy. Punishments then have the possibility of being renegotiation-proof since insiders relish the opportunity to become a legitimate leader rather than an insider and thus cannot be dissuaded from mounting a coup against an illegitimate leader by the offer of renegotiation.

This logic applies more generally, but it should be noted that there are parametric limits within which such a renegotiation-proof construction can exist. For example, the one outlined in the paragraph above fails to do so at any \( p < p^\ast \). More generally, the structure of the game imposes limits on how great the differences between continuation values of disciplining and opportunistic coups can be. And as the following proposition shows, there are always regions of the parameter space where such limits bind.

**Proposition 5.** There does not exist a renegotiation-proof power-sharing equilibrium if incumbents enjoy insufficient bias: specifically, for \( p < p^{**} \) where \( p^{**} \) is a constant that depends only on \((\gamma, \delta)\). Furthermore, \( p^{**} \) is decreasing in \( \gamma \) and \( p^{**} > 0 \) if \( \gamma < 1/2 \).

The proposition establishes a region of the parameter space where renegotiation-proof power sharing is not possible. Intuitively, renegotiation proofness necessitates that punishments imposed on leaders who violate the dictates of a randomization device must be preferred by the insider to letting by-gones be by-gones and reverting back to the equilibrium

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31Since transfers are zero in the democracy phase of the minimal democracy equilibrium if \( p < p^\ast \), insiders strictly prefers their equilibrium payoff (without coups) to that arising from mounting a coup. But, in the example, this is precisely the choice confronting an insider in a power-sharing equilibrium in the event that the leader refuses to step down. A coup would allow them to rule as a legitimate leader, but the offer of returning back to the equilibrium path peacefully would be preferred to carrying out the coup. Therefore the equilibrium can not be renegotiation-proof.
This, in general, requires that following a leader’s violation of power-sharing, the value to undertaking a coup and becoming leader is sufficiently high relative to that of remaining an insider. But the value of being a leader is limited by the fact that insiders can never receive strictly less than what they could obtain by undertaking constant coups. This yields a natural upper bound on how much the value of being a leader can exceed the value of being an insider along any continuation path of the game. When $p$ is low, i.e., when the randomization device calls for leaders and insiders to turnover relatively regularly, the value of being a leader is relatively close to that of an insider. In that case, remaining a peaceful insider rather than undertaking a coup against a recalcitrant leader is always so attractive that coups are never preferred over reversion back to the equilibrium path.

We explore in the appendix the parameter values under which this restriction has the most bite. As the proposition establishes, this tends to be when values of both $p$ and $\gamma$ are low. Having a low $p$ makes reversion back to the equilibrium path relatively attractive and renegotiation proofness harder to achieve. A low $\gamma$ makes the threat of a coup weaker, hence also favouring renegotiation back to the path. The fact that this occurs for low values of $p$ is particularly vexing, since it is the low values of $p$ that correspond most closely to turn taking. For instance the limiting case of $p = 0$ where the elite would alternate in the leadership position each period would seem a natural focal point of power-sharing. The proposition establishes that these cases are indeed the most difficult to sustain as power-sharing equilibria – more specifically that the minimalist democracy equilibrium at low values of $p$ is more likely to fall in the parameter range where power-sharing equilibria cannot be renegotiation proof than are equilibria at higher values of $p$.

To summarize, elections are more than a simple randomization device. Voters who are unwilling to vote for violators of previous elections play an important role. Their arm’s length relationship to the elite skirts issues of renegotiation that would undermine power-sharing amongst elites without voters. Alternative power-sharing strategies based on some other randomization device can be constructed without such third parties. But these will either lean heavily on strong informational assumptions: that opportunistic coups can be distinguished from disciplining coups, or will fail to be renegotiation-proof. Furthermore, renegotiation-proof power-sharing equilibria will sometimes fail to exist even under these strong assumptions. This is particularly likely for low values of $p$ – for instance if elite are supposed to take turns and turn over each period. In contrast, elections – in a minimalist democracy Markov equilibrium – use voters as a type of randomization device (one that cannot be used again if violated), support power sharing in a renegotiation-proof manner and, most importantly, do so without requiring agents to know anything about the reasons for coups.

Incidentally, for lower $\gamma$s where coups are less attractive, transfers to insiders on the equilibrium path are also low, suggesting that the value of reversion back to the equilibrium path should also fall with a decline in $\gamma$. But lowering $\gamma$ further in this region has minimal effect on the continuation value for a peaceful insider since their transfers are zero already.
5 Democratization and Empirical Implications

The preceding analysis reveals how autocratic and democratic equilibria coexist. This is due to a dynamic complementarity whereby the optimal action for today’s leader depends on the anticipated actions of future leaders.\footnote{A similar dynamic complementarity also arises with the voting decisions of citizens within the context of an established democracy. This has been analyzed by Myerson (2006) who shows how modifications of the game can help select the democratic equilibrium and Bidner and Francois (2013) who analyze the role of leaders in shifting norms towards equilibrium where leaders are responsive to voters.} If the current leader believes that future leaders will not respect election results, then this belief is self-reinforcing; it is a best response for the current leader to also not do so (part 2 of Lemma 1). This is why there always exists an autocratic equilibrium whereby turnover only occurs through leader death (violent or peaceful) and the democratic machinery lies dormant (Proposition 1). At the same time, a democratic alternative may also exist (under the conditions stated in Propositions 2 and 3). Here, where the patronage value of the state is not too high, and provided the electoral system delivers appropriate chances for electoral turnover, a confidence that future leaders will respect elections becomes self-enforcing as well. As such the current leader voluntarily steps aside too when losing elections, and violent challenges to power disappear.

One approach to understanding the process through which democracy emerges or disappears involves examining the elites’ equilibrium payoff under each regime. The potential benefit of democratization to leaders who are free to rule as they please is that, when credible, it helps solve the non-divisibility of the spoils of leadership problem. It is the non-divisibility of (at least a partial aspect of) power or prestige – which we have modelled through the utility term $F$ – that generates leadership insecurity here. The converse implication is that if leading a state generates neither power, prestige nor any other non-transferable benefit, an autocratic leader will always be able to devise a means of transferring the state’s divisible benefits to those who threaten him so that peace will ensue and autocratic power will persist. But with a non-divisible component of leadership this is no longer the case, and as we have shown, offering insiders a peaceful, stochastic avenue to power through elections may stop them using the (costly) coup technology. The following result establishes that doing so in fact makes both the leader and insiders strictly better off.

**Proposition 6.** The democratic equilibrium generically strictly Pareto dominates the autocratic equilibrium. In the special case where $\psi = \mu_2$ we have $V^L_D = V^L_A$ and $V^N_D = V^N_A$, otherwise $V^L_D > V^L_A$ and $V^N_D > V^N_A$.

The proposition suggests that if the elite have some capacity to coordinate on their desired equilibrium, they will choose democracy whenever it is feasible. This has two interesting implications.

First, it highlights how our minimalist approach to democracy contrasts with existing perspectives. Here the elite enthusiastically establish and respect elections without being compelled by outsiders (citizens, the poor, the masses, etc.). In contrast, Acemoglu and Robinson (2006) describe how elites establish and respect elections as the only feasible means to appease citizens and avoid revolution. Fearon (2011) describes how citizens’ rebellion threats lead the elite to respect elections, but it is not clear that elites are interested in establishing...
an electoral system, because of the existence of preferred equilibria without elections.\textsuperscript{34}

Second, it provides a rationale for why the elite may have self-interested motives for engaging in reforms of the state that lower patronage. For values of patronage that are close to, but not sufficiently low that democracy can be sustained, leaders would benefit by a decline in patronage putting them into the region where a democratic equilibrium exists. In short, destroying patronage renders tyrants insecure, thereby making democracy possible and thus helping engineer democratic transitions.

5.1 Empirical Implications

Due to the configuration of equilibria, a direct empirical implication of the present paper is that a permanent increase in graft to a sufficiently high level threatens democracy; it will always force democracy into autocracy. The fact that the democratic equilibrium strictly Pareto dominates the autocratic one suggests a reason for why elites would choose to coordinate on democracy whenever it is feasible. Thus, if we expect that political elite are able to coordinate on the preferred equilibrium, we predict democratization – in the minimalist sense – following a decline in graft. This is consistent with the pattern described by Jensen and Wantchekon (2004):

“... most African resource-dependent countries were authoritarian governments and struggled with democratic consolidation after the “third wave” of democratization. These resource-dependent countries include Algeria, Nigeria, Libya, Gabon, Cameroon, and the former Zaire. Besides South Africa, the transition to democracy has been successful only in resource-poor countries such as Benin, Mali, Senegal, and Madagascar.”

These perspectives are also reflected in the data. A large literature on the resource curse, which resonates with our theoretical model, focuses on resource abundance as an obstacle to inclusive institutions and democratization.\textsuperscript{35} This literature has investigated both permanent and temporary resource shocks.

Our model speaks to such systematic empirical regularities. Although we do not regard what we offer in this section as a formal test of the model, we underscore how our theoretical setup can jointly reconcile these additional moments in the data with the set of empirical regularities we have reported in Section 2.

Specifically, defining $y_t$ the level of state resources available in year $t$, a shock $\epsilon_t$ has the feature of permanence when affecting future expected resources available in the indefinite future, i.e. $\epsilon_t$ affects $E_t[y_{t+1}], E_t[y_{t+2}]$, and so on. These are the shocks which are close to changes in resources $U$ in our model; patronage available to fend off coup threats needs to

\textsuperscript{34}For instance, there is always a dictatorial equilibrium in which leaders provide nothing and rebellions never occur, regardless of whether there are elections. This is the best possible equilibrium for the leader, implying that democracy hinges on the elite being unable to select equilibria.

\textsuperscript{35}By focusing on the process of democratic transition our model complements other theoretical contributions more focused on drawing a characterization of the political processes that sustain the resource curse, as in Robinson, Torvik and Verdier (2006).
be permanently changed in order to compare different equilibrium characterizations.\(^{36}\) As an instance of such shocks, consider the case of an oil-rich country. Given that international oil prices follow a random walk,\(^ {37}\) \(y_t = y_{t-1} + \epsilon_t\), a negative shock \(\epsilon_t\) permanently reduces expected oil revenues at any future \(t + j\), for \(j = 1, 2, 3...,\) since \(E_t[y_{t+j}] = y_t\). Along these lines, Caselli and Tesei (2011) focus on permanent resource windfalls due to improvements in the international price of the main commodity exported by a country. Such commodity prices typically follow nonstationary processes and therefore \(\epsilon\) shocks have persistent effects. The authors show that increases in commodity prices (and hence revenues from exports) tend to consolidate autocracies. Given the inherently divisible and transferable nature of natural resources, commodity shocks are particularly close to our setup in terms of shocks to \(\psi\), the availability of patronage, an issue amply discussed in the literature (Torvik, 2002; Collier and Hoeffler, 2005). Tsui (2011) focuses on historical discoveries of large oil reservoirs as an important determinant of long-run autocratic drift in a large panel of countries. Wantchekon (1999) discusses the political dynamics around peak discovery in the case of Nigeria along these same lines. Brückner, Ciccone, and Tesei (2012) focus on oil revenue windfalls as well, but with opposite results relative to Caselli and Tesei (2011) and Tsui (2011). In fact, studies of resource shocks and their effects on political institutions have received criticism.\(^ {38}\)

On the other hand, a shock \(\epsilon_t\) is temporary if it has the feature of leaving expected resources available in the indefinite future unchanged, i.e. \(\epsilon_t\) does not affect \(E_t[y_{t+1}], E_t[y_{t+2}],\) and so on. This is consistent with Acemoglu and Robinson’s (2001, 2006) ‘window of opportunity’ view of transitions that allows for a boom period of \(y_t = h > 0\) with probability \(1-s\) and recession \(a<h< h\) with probability \(s\), which ultimately has the effect of changing the opportunity cost of transitions. In this setting economic shocks occur independently and the resource process is stationary. Brückner and Ciccone (2011) focus on these temporary resource shocks, specifically droughts in Africa, and show that low rainfall shocks (i.e. negative transitory shocks) tend to predict democratizations consistently with Acemoglu and Robinson (2001, 2006).

We scrutinize similar empirical evidence to the literature in the context of our model in Table 4, which looks at triggers of political transitions. The analysis here is kept brief and essentially focused on confirming whether negative resource shocks act to move autocratic systems towards democracy, and more specifically towards competitive elections and minimalist democracy, in contrast with other democratic features less related to our theory, such as political inclusiveness.

We employ specifications close to the reduced-form regressions of Brückner and Ciccone (2011, Eq. 2), including jointly permanent (resource prices) and temporary (weather) shocks. While our theory relies on the former, omitting the role of the latter, which have been shown to be relevant in past research, could bias the analysis. Table 4 employs a country and year fixed effects specification (plus country specific linear time trends) of the change between year \(t\) and \(t+1\) of four institutional dependent variables: the Polity 2 score, electoral competitiveness, political inclusiveness, and executive constraints. The set of independent variables

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\(^{36}\)This remark follows from the fact that our current model does not focus on shocks to \(U\) that are expected to be temporary in nature although it can be extended in this direction.

\(^{37}\)Brückner, Ciccone, and Tesei (2012).

\(^{38}\)See for instance Wacziarg (2012).
of interest includes the price growth of the main commodity exported by a country based on United Nation’s Comtrade data (following the protocol spelled out by Caselli and Tesei, 2011) and the log Global Precipitation Climatology Project rainfall estimates at time \( t \) and at time \( t - 1 \). The sample coincides with the set of Sub-Saharan African countries identified by Brückner and Ciccone for which we have commodity quantities and prices.

Column 1 of Table 4 can be seen as a replication and robustness check of Brückner and Ciccone (2011) or of Caselli and Tesei (2011). It shows that resource shortfalls, in terms of lower rainfalls or lower commodity prices, strengthen the level of democracy by significantly increasing the Polity 2 overall score. Both temporary and permanent shocks appear to matter in this reduced-form environment. Quantitatively, the effect of one standard deviation drop in log rainfall at \( t - 1 \) (−0.57) implies an increase of 1.4 Polity 2 points. A one standard deviation decrease in commodity price growth between \( t \) and \( t - 1 \) (−0.23) produces an increase of 0.2 Polity 2 points and a one standard deviation fall in commodity price growth between \( t - 1 \) and \( t - 2 \) (−0.22) produces an increase of 0.23 Polity 2 points. Consistently with our discussion in Section 3, electoral competitiveness appears to respond statistically to resource shortfalls. Both commodity price declines and droughts increase electoral competitiveness in column 2, pushing autocracies towards minimalist democracies. Importantly for our theory, this does not happen for political inclusiveness measures (statistically insignificant and very noisy in column 3), which more properly pertain to fully representative (as opposed to minimalist) democracies.\(^{39}\) In column 4 executive constraints appear to respond weakly to rainfall shocks and do not systematically respond to resource shocks. This ambiguity is not surprising, as in Figure 6 executive constraints show an uptake in between electoral competitiveness and inclusiveness. Columns (5) to (8) show the robustness of our findings to the exclusion of Polity IV interregnum periods, as those periods require interpolation of Polity 2 scores and could be overly influential around periods of political transition.

In synthesis, Table 4 reiterates evidence for the view that resource value declines seem to push autocratic regimes toward democratization. But importantly, this appears true along the electoral competitiveness dimension and for declines that affect the permanent value of state resources, both features that are central to our analysis.

6 Conclusions and Future Directions

After positing a relevant set of stylized facts, some of which are novel, this paper studies political transitions in to and out of democracy based on the minimalist concept of Schumpeter (1942) and Przeworski (1999). The focus is the mere presence of competitive elections. The fact that elections allow a stochastic rent sharing from executive power to elites currently not in power can lead them to eschew coup opportunities. When the respect of such electoral outcomes is credible for leaders, elections can reduce losses to the elite as a whole that arise from coups d’état. These are distinctive advantages of hybrid systems which feature minimalist democracy and are a valuable avenue for autocratic leaders who cannot fend off coup threats with side payments.

\(^{39}\)Although suggestive, the combination of coefficient magnitude and considerable noise in the estimates for Inclusive politics does not allow however to pinpoint ‘precise zeros’.
The main contribution of the paper is to shed light on the relevance of a set of hybrid regimes – electoral democracies with drastically low inclusiveness and limited constraints on the executive – as a first step in the process of democratic transition. This exercise should therefore be interpreted as moving away from a coarse definition of a polity as purely democratic or purely autocratic, but rather as transiting through different hybrid phases, of which “electoral competition” represents a first basic stepping stone decoupled from any requirement of representation. We believe this is an important departure from the literature and highly relevant for a large number of the world’s weak polities that lie between these two extreme poles. The Minimalist Democracies that we have studied embody elements from both ends of the political schema. Their underlying context is one in which power would seem to be determined by force, as the institutions in such countries are weak. Yet leaders hold elections, and even leave power when they lose. In these democracies, leaders who control violence, and hence sufficient force to stay in power, choose to step aside and respect electoral outcomes. We have first established why a dictator, in control of power through force, would choose to implement a minimalist democracy. Relatedly we have demonstrated how the process of holding elections can serve a substantive function when the leader – controlling force – can always choose to annul results and remain in office.

Secondly, we have developed the conditions under which minimalist democracy may emerge. By offering a probabilistic share of future leadership spoils to insiders, leaders in minimalist democracies can obtain peace and security from attempts against their regime. Additionally, they can pay (from the patronage available to them) insiders who would threaten them less in democracies than they would have to in autocracies in order to secure peace. Importantly, however, we have demonstrated that reducing patronage transfers is never a sufficient motivation for minimalist democracy to be implemented by a leader. Democracy can only be sustained if leaders fear that by flouting democratic rules they will face immediate threats to the stability of their regime. An important lesson here then is that: Peaceful democracy rests on violent threats – necessarily. If these threats against recalcitrant leaders can be mitigated – as they are when sufficient graft is available – then democracy can never be sustainable.

Thirdly, the paper has extensively explored the conditions under which voters are, and are not, replaceable by a randomization device that would allow the elite an alternative way to peacefully share power. In general a minimalist democracy with elections and voters cannot be replicated by such a device when either there is less than full information about the factors that would precipitate violent attempts to take over power, or where the elite wish to share so much of the value of being a leader amongst themselves that the value of being a leader is close to the value of being an elite insider.

There is a final question that naturally follows from this analysis. Here we provide some conjectures about it but leave to future research a fuller analysis. Does this framing of the emergence of minimalist democracy tell us anything about the process by which minimalist democracy turns in to a fully-fledged or consolidated democracy? The process we have analyzed points to some intriguing possibilities. The threat of force sustains a commitment to patronage transfers in autocracies. To ensure that their current share of spoils extends in to the future, elites thus only need to sustain that threat through maintaining their power-base – i.e., through their links to the rank-and-file. However, as we have seen, this threat of force
does not guarantee graft transfers in minimalist democracies since a probabilistic share of leadership benefits replaces it. This contrasts with autocracies where the very lack of institutional commitments to sharing power ensure a credible commitment on the autocrat’s part to share graft. Democratic contests between political elites thus supplant the role that graft transfers from the leader to political elites perform in autocracy.

A plausible conjecture would thus be that the transition to minimalist democracy gives rise to the possibility of a new form of political actor to occupy elite roles. In autocracies, the political elites are those able to mobilize (potentially violent) support. The threat they pose must be placated by autocrats seeking security through transfers of graft. After minimalist democratic transitions, violent threats are ameliorated by democratic participation – elites eschew coup opportunities and instead participate in electoral politics. Since graft transfers fall (and often disappear) in minimalist democracies, the resources that would enable elites to maintain the support of the rank-and-file through the allocation of patronage dry up. The political elite who control violence shift from being key players with a claim to resources into marginal players through whom resources need not ever flow. We believe that this transition may play an important role in allowing the emergence of an alternative, non-violent and rival form of elite who are able to offer policy benefits (in lieu of graft) to the rank-and-file in return for their support. We explore this conjecture in future work.
A Further Details

A.1 Markov Perfect Equilibrium

A Markov strategy for the leader involves a state-contingent transfer offer \( \tau_\omega \in [0, U] \), and a state-contingent indicator of whether elections are respected, \( z_\omega \in \{0, 1\} \). For ease of presentation we impose the fact that a leader would never want to step down in state \( \omega_0 \) i.e. \( z_{\omega_0} = 0 \) (the proof is provided in section A.2 below). Furthermore, our focus on pure strategies for the leader reflects our primary interest in autocratic and democratic equilibria. Thus, a Markov strategy for the leader is given by three numbers \( \sigma_L \equiv \{\tau_{\omega_p}, \tau_{\omega_0}, z_{\omega_p}\} \).

The strategy for an insider involves a state-contingent probability of mounting a coup following each possible transfer, \( c_\omega(\tau) \in [0, 1] \), for \( \omega \in \{\omega_p, \omega_0\} \) and \( \tau \in [0, U] \). Thus, a Markov strategy for the non-leader is given by a pair of functions \( \sigma_N \equiv \{c_{\omega_p}(\tau), c_{\omega_0}(\tau)\} \).

Given these, we can derive value functions as follows. In state \( \omega_p \), the value of being a leader at the start of the period, \( V_{\omega_p}^L \), the value of being a leader following an election loss, \( \tilde{V}_{\omega_p}^L \), and the value of being a non-leader faced with a transfer offer of \( \tau \), \( V_{\omega_p}^N(\tau) \), satisfy:

\[
V_{\omega_p}^L = \max_{\tau \in [0, U]} \left\{ F + U - \tau + (1 - \delta) \cdot c_{\omega_p}(\tau) \cdot (1 - \gamma) \cdot V_{\omega_p}^L + (1 - c_{\omega_p}(\tau)) \cdot [p \cdot V_{\omega_p}^L + (1 - p) \cdot \tilde{V}_{\omega_p}^L] \right\}
\]

(18)

\[
\tilde{V}_{\omega_p}^L = \max_{z \in [0, 1]} \left\{ z \cdot V_{\omega_p}^N(\tau_{\omega_p}^*) + (1 - z) \cdot V_{\omega_p}^L \right\}
\]

(19)

\[
V_{\omega_p}^N(\tau) = \max_{c \in [0, 1]} \left\{ c \cdot [(1 - \delta) \cdot \gamma \cdot V_{\omega_p}^L + (1 - c) \cdot (\tau + (1 - \delta) \cdot [p \cdot V_{\omega_p}^N(\tau_{\omega_p}^*) + (1 - p) \cdot \tilde{V}_{\omega_p}^N]) \right\}
\]

(20)

where \( \tilde{V}_{\omega_p}^N \) is the value of being a non-leader following an election victory:

\[
\tilde{V}_{\omega_p}^N \equiv z_{\omega_p}^* \cdot V_{\omega_p}^L + (1 - z_{\omega_p}^*) \cdot [(1 - \delta) \cdot V_{\omega_p}^N(\tau_{\omega_p}^*) + \delta \cdot V_{\omega_p}^N(\tau_{\omega_p}^*)]
\]

(21)

and \( \tilde{\omega} \) is the state next period following a refusal to respect an election:

\[
\tilde{\omega} \equiv \begin{cases} 
\omega_p & \text{if } z_{\omega_p}^* = 0 \\
\omega_0 & \text{if } z_{\omega_p}^* = 1 
\end{cases}
\]

(22)

In state \( \omega_0 \), we use the fact that \( z_{\omega_0}^* = 0 \), to get the analogous value functions:

\[
V_{\omega_0}^L = \max_{\tau \in [0, U]} \left\{ F + U - \tau + (1 - \delta) \cdot c_{\omega_0}(\tau) \cdot (1 - \gamma) \cdot V_{\omega_0}^L + (1 - c_{\omega_0}(\tau)) \right\}
\]

(23)

\[
V_{\omega_0}^N(\tau) = \max_{c \in [0, 1]} \left\{ c \cdot [(1 - \delta) \cdot \gamma \cdot V_{\omega_0}^L + (1 - c) \cdot [\tau + (1 - \delta) \cdot V_{\omega_0}^N(\tau_{\omega_0}^*) + \delta \cdot V_{\omega_0}^N(\tau_{\omega_0}^*)]] \right\}
\]

(24)

\footnote{Since elections only occur if there is no coup, the only prior action within the period is the transfer amount. We economize on extraneous notation by imposing that the leader respects an election with a probability that is independent of the specific transfer that dissuaded a coup. Nothing of substance would change if we allowed for randomization in the decision to respect elections, so we ignore this possibility for simplicity.}
The proposed strategy profile is an equilibrium profile if the components solve the problems posed on the right side of the above equations. That is:

\[ \tau_{\omega_0}^* \in \arg\max_{\tau \in [0, U]} \{ F + U - \tau + (1 - \delta) \cdot [c_{\omega_0}^* (\tau) \cdot (1 - \gamma) \cdot V_{\omega_0}^L + (1 - c_{\omega_0}^* (\tau)) \cdot [p \cdot V_{\omega_0}^L + (1 - p) \cdot \tilde{V}_{\omega_0}^L]] \} \] \hspace{1cm} (25)

\[ z_{\omega_0}^* \in \arg\max_{z \in [0, 1]} \{ z \cdot V_{\omega_0}^N (\tau_{\omega_0}^*) + (1 - z) \cdot V_{\omega_0}^L \} \] \hspace{1cm} (26)

\[ c_{\omega_0}^* (\tau) \in \arg\max_{c \in [0, 1]} \{ c \cdot [(1 - \delta) \cdot \gamma \cdot V_{\omega_0}^L] + (1 - c) \cdot [\tau + (1 - \delta) \cdot [p \cdot V_{\omega_0}^N (\tau_{\omega_0}^*) + (1 - p) \cdot \tilde{V}_{\omega_0}^N]] \} \] \hspace{1cm} (27)

\[ \tau_{\omega_0}^* \in \arg\max_{\tau \in [0, U]} \{ F + U - \tau + (1 - \delta) \cdot [c_{\omega_0}^* (\tau) \cdot (1 - \gamma) \cdot V_{\omega_0}^L + (1 - c_{\omega_0}^* (\tau)) \cdot V_{\omega_0}^L] \} \] \hspace{1cm} (28)

\[ c_{\omega_0}^* (\tau) \in \arg\max_{c \in [0, 1]} \{ c \cdot [(1 - \delta) \cdot \gamma \cdot V_{\omega_0}^L] + (1 - c) \cdot [\tau + (1 - \delta) \cdot [p \cdot V_{\omega_0}^N (\tau_{\omega_0}^*) + (1 - p) \cdot \tilde{V}_{\omega_0}^N]] \} \] \hspace{1cm} (29)

**Definition 1.** A Markov Perfect Equilibrium is a profile of Markov strategies, \( \sigma^*_T \) and \( \sigma^*_N \), such that (18) to (29) simultaneously hold.

**A.2 It is never optimal to step down in state \( \omega_0 \): \( z^*(\omega_0) = 0 \)**

Suppose that the leader in state \( \omega_0 \) stepped down. Then since voters still perceive the leader to be a tyrant, and since we take \( \eta \to 0 \), they will (almost surely) lose an election against the new leader. Since the incumbent wins with probability 1, label such a state \( \omega_1 \). Since the leader in this state always wins elections, and since we take \( \eta \to 0 \), the leader (almost surely) can not take actions that change citizen beliefs. As such, the state remains at \( \omega_1 \) until the original leader (i.e. the perceived tyrant) dies. Upon this death, the replacement would become a tyrant with probability \( \epsilon \) upon taking the leadership and thus citizens once again become indifferent between the candidates. That is, there is a return to state \( \omega_0 \).

A successful coup in state \( \omega_1 \) delivers a continuation value of \( V_{\omega_0}^L \) (since the coup instigator is still perceived to be a tyrant). Thus, the value of being the insider in state \( \omega_1 \) satisfies the following:

\[ V_{\omega_1}^N = c_{\omega_1}^* \cdot [(1 - \delta) \cdot \gamma \cdot V_{\omega_1}^L] + (1 - c_{\omega_1}^*) \cdot [\tau_{\omega_1}^* \cdot (1 - \delta) \cdot V_{\omega_1}^N] \] \hspace{1cm} (30)

where \( \tau_{\omega_1}^* \) is the equilibrium transfer, and \( c_{\omega_1}^* \equiv c_{\omega_1}^* (\tau_{\omega_1}^*) \) is the equilibrium probability of mounting a coup, in state \( \omega_1 \).

**Result 1.** The leader in state \( \omega_0 \) will never want to step down: i.e. \( V_{\omega_1}^N < V_{\omega_0}^L \).

**Proof.** The result will follow by establishing that \( V_{\omega_1}^N = (1 - \delta) \cdot \gamma \cdot V_{\omega_0}^L \). If \( c_{\omega_1}^* = 1 \) then this is obvious from (30). If \( c_{\omega_1}^* < 1 \), then \( \tau_{\omega_1}^* > 0 \) (if instead \( \tau_{\omega_1}^* = 0 \), then the implied value of \( V_{\omega_1}^N \) would be zero, making a coup strictly preferable). But then \( \tau_{\omega_1}^* \) must be set at that critical transfer value that makes the non-leader indifferent to a coup. Thus, for any possible value of \( c_{\omega_1}^* \) we have \( V_{\omega_1}^N = (1 - \delta) \cdot \gamma \cdot V_{\omega_0}^L \), so that \( V_{\omega_1}^N < V_{\omega_0}^L \) as required. \( \square \)
B Supporting Results

Result 2. In any minimalist democracy equilibrium we have $V^L_D > V^N_D$.

Proof of Result 2:

Proof. In any minimalist democracy equilibrium it is either the case that $\tau_D > 0$ or $\tau_D = 0$.

If $\tau_D > 0$, then $\tau_D = \hat{\tau}_D$ which ensures $V^N_D = \gamma \cdot (1-\delta) \cdot V^L_D < V^L_D$. If instead $\tau_D = 0$, then the value functions (11) and (12) imply $V^L_D > V^N_D$. To see this, note that $V_D \equiv V^L_D + V^N_D = (F + U)/\delta$. This implies $V^N_D = V_D - V^L_D$, which can be substituted into (11) and solved to get $V^L_D = \frac{\delta \cdot (1-\delta)(1-\gamma)}{F+U} \cdot V_D$. Since $\delta > 0$ implies the first fraction is greater than unity, it follows that $V^L_D > V_D/2$ and thus that $V^L_D > V^N_D$ as required. Thus, in all cases we have $V^L_D > V^N_D$. \(\square\)

Lemma 6. A leader in the tyranny state avoids coups whenever strictly feasible. That is, $\hat{\tau}_T < U \Rightarrow c_T = 0$.

Proof of Lemma 6

Proof. The result is obvious if $\hat{\tau}_T \leq 0$ since coups can be avoided for free. Suppose then that $\hat{\tau}_T \in (0, U)$. The strategy is to show that (i) there is no profitable deviation from $\tau_T = \hat{\tau}_T$ and (ii) there is always a profitable deviation from any $\tau_T \neq \hat{\tau}_T$. This will establish that $c_T = 0$ since strict feasibility implies that leaders can offer infinitesimally more than $\hat{\tau}_T$ and ensure that insiders coup with probability zero.

Suppose that $\tau_T = \hat{\tau}_T \in (0, U)$. There is a profitable deviation only if it is profitable to deviate to $\tau = 0$: it is never profitable to deviate to any $\tau \in (\hat{\tau}_T, U]$ since coups are still avoided but at a higher cost, and any deviation to some $\tau \in (0, \hat{\tau}_T)$ is dominated by $\tau = 0$ since coups are still not avoided but at a lower cost. Since it will induce a coup for sure, it is not profitable to deviate to $\tau = 0$ if $V^L_T \geq F + U + (1-\gamma) \cdot (1-\delta) \cdot V^L_T$. That is, we need to show that

$$V^L_T \geq \frac{\delta}{\delta + \gamma \cdot (1-\delta)} \cdot \frac{F + U}{\delta}$$

(31)

whenever $\tau_T = \hat{\tau}_T \in (0, U)$. To this end, note that $\tau_T = \hat{\tau}_T$ implies that insiders are indifferent to holding a coup. Since the expected payoff to a coup is the same as in the democracy state (i.e. becoming a democratic leader), the fact that there are no coups in democracy implies $V^N_D \geq \gamma \cdot (1-\delta) \cdot V^L_D = V^N_T$. Note too that $\tau_T = \hat{\tau}_T < U$ implies insiders coup with probability zero. Using $c_T = 0$ along with $V^N_D \geq V^N_T$ in (14) gives $V^N_T \geq \hat{\tau}_T + (1-\delta) \cdot V^N_T$. Use this along with (13) to get $V_T \equiv V^L_T + V^N_T \geq \frac{F + U}{\delta}$. Since $V^L_D + V^N_D = \frac{F + U}{\delta}$, we have $V^L_T + V^N_T \geq V^L_D + V^N_D$. This, along with $V^N_D \geq V^N_T$ implies $V^L_T \geq V^L_D$. We therefore have $V^L_T = V_T - V^N_T = V_T - \gamma \cdot (1-\delta) \cdot V^L_T \geq \frac{F + U}{\delta} - \gamma \cdot (1-\delta) \cdot V^L_T$. Rearranging gives $V^L_T \geq \frac{1}{1+\gamma \cdot (1-\delta)} \cdot \frac{F + U}{\delta}$. Condition (31) follows from noting that $\frac{1}{1+\gamma \cdot (1-\delta)} > \frac{\delta}{\delta + \gamma \cdot (1-\delta)}$.

Suppose that $\tau_T \neq \hat{\tau}_T \in (0, U)$. There is clearly a profitable deviation to $\tau = \hat{\tau}_T$ if $\tau_T \in (\hat{\tau}_T, U]$ and to $\tau = 0$ if $\tau_T \in (0, \hat{\tau}_T)$. Thus, if there is an equilibrium with $\tau_T \neq \hat{\tau}_T \in (0, U)$ then it must be $\tau_T = 0$. In this case insiders coup with probability one since $\tau_T = 0 < \hat{\tau}_T$. Using $c_T = 1$ and $\tau_T = 0$ in (9) tells us that the equilibrium value of being a tyrant is given by the right side of (31). But this can not be an equilibrium since there is a profitable deviation to choosing $\tau_T = \hat{\tau}_T$ for all future periods. This will ensure that there are no coups and therefore the payoff to this strategy coincides with the value of $V^L_T$ derived above in the case where $\tau_T = \hat{\tau}_T$.\(\square\)
$\hat{\tau}_T \in (0, U)$. That is, the left side of (31). The fact that this represents a profitable deviation follows from noting that we proved above that (31) holds with a strict inequality.

Therefore if $\hat{\tau}_T \leq 0$ then it is clearly optimal to set $\tau_T = 0$ and $c_T = 0$ as a result. If $\hat{\tau}_T \in (0, U)$, we have shown that the only equilibrium has $\tau_T = \hat{\tau}_T$ and since $\hat{\tau}_T < U$ it must be that $c_T = 0$ in this case also. Thus $\hat{\tau}_T < U \Rightarrow c_T = 0$.

**Result 3.** Democratic equilibria with differing transfer levels never coexist.

**Proof.** Lemma 3 establishes that if parameters are in $P_1$, then a democratic equilibrium must have $\tau_D = 0$. Thus, the only possible way for there to be multiplicity is if equilibria with different positive transfer levels co-exist (and thus parameters are in $P_2$). But if there is an equilibrium with transfers $\tau_D = \tau'$, then parameters must be such that $\tau' = \hat{\tau}_D$, where $\hat{\tau}_D$ is given by (33) where $\{V^L_D, V^N_D\}$ are computed from (11) and (12) using $\tau_D = \tau'$. The resulting condition has a unique solution for $\tau'$, so that an equilibrium with a transfers of $\tau' > 0$ precludes there being an equilibrium with any other transfer. □

**C Proofs**

**Proof of Lemma 1:**

**Proof.** From (3) we have:

$$\hat{\tau}_A \equiv (1 - \delta) \cdot \left[ \gamma \cdot V^L_A - V^N_A \right]. \quad (32)$$

1. We proceed by showing that $\hat{\tau}_A < U$ implies that (i) there are no profitable deviations from choosing $\tau = \hat{\tau}_A$, and (ii) there is always a profitable deviation from choosing any $\tau \neq \hat{\tau}_A$.

Suppose $\hat{\tau}_A < U$ and that $\tau_A = \hat{\tau}_A$. Since $\hat{\tau}_A < U$, it must be that there are no coups in equilibrium (otherwise raising $\tau$ by a marginal amount will cause coups to occur with probability zero). If there is a profitable deviation, it will be to setting $\tau = 0$. This will definitely induce a coup (since $\tau = 0 < \hat{\tau}_A$). Thus, there is not a profitable deviation if

$$F + U + (1 - \delta) \cdot (1 - \gamma) \cdot V^L_A \leq V^L_A.$$

That is, if

$$V^L_A \geq \frac{F + U}{1 - (1 - \delta)(1 - \gamma)} = \frac{\delta}{\delta + \gamma \cdot (1 - \delta)} \cdot \frac{F + U}{\delta}.$$

Using $c_A = 0$ along with (32) in (5) gives $V^N_A = \gamma \cdot (1 - \delta) \cdot V^L_A$. Adding (4) and (5) and re-arranging gives

$$V_A \equiv V^L_A + V^N_A = \frac{F + U}{\delta}.$$

Therefore $V^L_A = V_A - V^N_A = V_A - \gamma \cdot (1 - \delta) \cdot V^L_A$, so that

$$V^L_A = \frac{1}{1 + \gamma \cdot (1 - \delta)} \cdot V_A = \frac{1}{1 + \gamma \cdot (1 - \delta)} \cdot \frac{F + U}{\delta} \geq \frac{\delta}{\delta + \gamma \cdot (1 - \delta)} \cdot \frac{F + U}{\delta},$$

as required. Thus, there are no profitable deviations from $\tau = \hat{\tau}_A$. 38
Now suppose that $\tau_A \neq \hat{\tau}_A$. If $\tau_A > \hat{\tau}_A$ then $\tau = \hat{\tau}_A$ is clearly a profitable deviation (it achieves coups with the same probability, zero, at a lower cost). Similarly, if $\tau_A \in (0, \hat{\tau}_A)$ then $\tau = 0$ is clearly a profitable deviation (it achieves coups with the same probability, one, at a lower cost). The only remaining possibility is $\tau = 0$. To show that there is a profitable deviation consider a deviation to $\tau = \hat{\tau}_A$. If this is a profitable deviation, then it must be that

$$F + U - \hat{\tau}_A + (1 - \delta) \cdot V_A^L > V_A^L.$$ 

That is, if

$$F + U > \hat{\tau}_A + \delta \cdot V_A^L$$

Use the fact that $V_A^N = \gamma \cdot (1 - \delta) \cdot V_A^L$ to get $\gamma \cdot V_A^L = V_A^N / (1 - \delta)$ which can then be used in (32) to get $\hat{\tau}_A = V_A^N / (1 - \delta) \cdot V_A^N = \delta \cdot V_A^N$. Using this in the above equation implies that we need to show

$$F + U > \delta \cdot [V_A^L + V_A^N].$$

Adding (4) and (5) and using $c_A = 1$ and $\tau_A = 0$, we get $V_A^L + V_A^N = F + U (1 - \delta) \cdot V_A^L$. That is,

$$F + U = \delta \cdot V_A^L + V_A^N > \delta \cdot [V_A^L + V_A^N],$$

as required. Thus, there can not be an equilibrium with $\tau_A = 0$ if $\hat{\tau}_A < U$.

An implication of this is that $\hat{\tau}_A < U$ implies a secure autocracy. But this is not so when $\hat{\tau}_A = U$. Insiders may hold coups with a positive probability when offered all available patronage: $\tau_A = \hat{\tau}_A = U$. If this coup probability is sufficiently low then leaders will opt to transfer everything and face a small coup probability. However, if this coup probability is sufficiently high then leaders will opt to transfer nothing and face coups with probability one. Of course, if $\hat{\tau}_A > U$ then it is impossible to dissuade insiders from mounting coups, and a strongly insecure autocracy is the only possibility.

2. Follows from $V_A^L \geq \gamma \cdot V_A^L > V_A^N$ where the first inequality follows from $\gamma \leq 1$ and the second inequality follows from the fact that $\hat{\tau}_A > 0$. To demonstrate the latter fact, suppose instead that we had $\hat{\tau}_A \leq 0$. Since $\tau \geq 0 \geq \hat{\tau}_A$ we must have $c = 0$. From the optimality conditions we have $\tau_A = 0$ since $\sigma_A(\tau) = 0$ for all $\tau$. Using this is the expressions for the value functions gives $V_A^N = 0$ and $V_A^L = (F + U) / \delta$. Thus, $\gamma \cdot V_A^L - V_A^N > 0$ which implies $\hat{\tau}_A > 0$ which is a contradiction.

$\square$

**Proof of Proposition 1:**

**Proof.** The strategy is to first characterize the set of parameters for which an autocratic equilibrium with $\hat{\tau}_A > U$, $\hat{\tau}_A < U$, and $\hat{\tau}_A = U$ exist. This will allow us to then characterize the set of parameters for which a secure, insecure, and partially secure autocratic equilibrium

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41If this were not true, then it could not be optimal for the leader to pay $\tau_A = \hat{\tau}_A$ since a marginally higher transfer would ensure a secure autocracy (achieving a discrete increase in benefit at a marginal increase in cost).
exists. Since these cases cover all possible autocratic equilibria and since the characterized parameter sets will be generically disjoint (two of the sets will share a boundary), it follows that autocratic equilibria are generically unique.

To this end, we begin by characterizing the set of parameters that support an autocratic equilibrium in which $\hat{\tau}_A > U$. Such equilibria must have insecure autocrats since the required transfer is infeasible. The parameter set is those for which $\hat{\tau}_A > U$, where $\hat{\tau}_A$ is given by (32) where $\{V^L_A, V^N_A\}$ are computed using $\tau_A = 0$ and $c_A = 1$. This gives $\psi < \mu_1$.

Next, we characterize the set of parameters that support an autocratic equilibrium in which $\hat{\tau}_A < U$. Such equilibria must have secure autocrats by the above lemma. The parameter set is those for which $\hat{\tau}_A < U$, where $\hat{\tau}_A$ is given by (32) where $\{V^L_A, V^N_A\}$ are computed using $\tau_A = \hat{\tau}_A$ and $c_A = 0$. This gives $\psi > \mu_2$.

Next, we characterize the set of parameters that support an autocratic equilibrium in which $\hat{\tau}_A = U$. We divide this case into three sub-cases.

1. The equilibrium will have a strongly insecure autocrat if and only if parameters satisfy $\hat{\tau}_A = U$, where $\hat{\tau}_A$ is given by (32) where $\{V^L_A, V^N_A\}$ are computed using $\tau_A = 0$ and $c_A = 1$ (offering $\tau = U$ is not a profitable deviation because we can have insiders holding a coup with probability one in this event, removing any incentive to offer more than zero). This gives $\psi = \mu_1$.

2. The equilibrium will have a secure autocrat if and only if parameters satisfy $\hat{\tau}_A = U$, where $\hat{\tau}_A$ is given by (32) where $\{V^L_A, V^N_A\}$ are computed using $\tau_A = U$ and $c_A = 0$ (offering $\tau = 0$ is not a profitable deviation for reasons identical to those given in lemma 1). This gives $\psi = \mu_2$.

3. The equilibrium will have a weakly insecure autocrat if and only if parameters satisfy $\hat{\tau}_A = U$, where $\hat{\tau}_A$ is given by (32) where $\{V^L_A, V^N_A\}$ are computed using $\tau_A = U$, the implied value of $c_A$ satisfies $c_A \in (0, 1)$, and we verify that there are no incentives to deviate to offering $\tau = 0$. This gives $\psi \in [\mu_1, \mu_2]$.

In summary then, a secure autocratic equilibrium exists if and only if $\psi \geq \mu_2$. A strongly insecure autocratic equilibrium exists if and only if $\psi \leq \mu_1$, and a weakly insecure autocratic equilibrium exists if and only if $\psi \in [\mu_1, \mu_2]$. Thus, autocratic equilibrium is unique unless $\psi = \mu_1$, in which case two equilibria exist (one weakly insecure and one strongly insecure).

**Proof of Lemma 2:**

**Proof.** From (8) we have

$$\hat{\tau}_D \equiv (1 - \delta) \cdot \{\gamma \cdot V^L_D - (p \cdot V^N_D + (1 - p) \cdot V^L_D)\}. \quad (33)$$

It is obvious that $\tau_D = 0$ if $\hat{\tau}_D \leq 0$, since the leader can dissuade coups for free. Consider a proposed democratic equilibrium in which $\hat{\tau}_D \in (0, U]$. Since coups are avoided in any democratic equilibrium, we have $\tau_D = \hat{\tau}_D$. From (33) and (12) we get $V^N_D = \gamma \cdot (1 - \delta) \cdot V^L_D$, and by adding (11) and (12) we get $V^L_D + V^N_D = (F + U)/\delta$.

If there is a profitable deviation, it is to $\tau = 0$ (which must incite a coup by virtue of $\hat{\tau}_D > 0$). Thus, there is not a profitable deviation if

$$F + U + (1 - \gamma) \cdot (1 - \delta) \cdot V^L_D \leq V^L_D,$$
but since \( V_D^N = \gamma \cdot (1 - \delta) \cdot V_D^L \), this is \( F + U \leq \delta \cdot V_D^L + V_D^N \). But this is ensured because

\[
F + U = \delta \cdot V_D^L + \delta \cdot V_D^N < \delta \cdot V_D^L + V_D^N,
\]

where the equality follows from \( V_D^L + V_D^N = (F + U)/\delta \).

\( \square \)

**Proof of Lemma 3:**

Proof. The strategy is to first prove the ‘only if’ statements. The second step is to note that the fact that \( P_1 \equiv \{ p, \delta, \gamma, U, F \mid p \leq p^* \} \) and \( P_2 \equiv \{ p, \delta, \gamma, U, F \mid p > p^*, \psi \geq f(p) \} \) are disjoint implies the ‘if’ conditions.

If a democratic equilibrium involves \( \tau_D = 0 \), then it must be the case that \( \hat{\tau}_D \leq 0 \), where \( \hat{\tau}_D \) is given by (33) where \( \{ V_D^L, V_D^N \} \) are computed from (11) and (12) using \( \tau_D = 0 \). This gives \( p \leq p^* \).

If a democratic equilibrium involves \( \tau_D \in (0, U) \) then \( \hat{\tau}_D \in (0, U) \), where \( \hat{\tau}_D \) is given by (33) where \( \{ V_D^L, V_D^N \} \) are computed from (11) and (12) using \( \tau_D = \hat{\tau}_D \). This gives \( p > p^* \) and \( \psi \geq f(p) \).

So far we have established that if there is a democratic equilibrium with zero transfers then parameters are in \( P_1 \equiv \{ p, \delta, \gamma, U, F \mid p \leq p^* \} \), and that if there is a democratic equilibrium with positive transfers then parameters are in \( P_2 \equiv \{ p, \delta, \gamma, U, F \mid p > p^*, \psi \geq f(p) \} \). But the fact that \( P_1 \) and \( P_2 \) are disjoint implies the ‘if’ conditions. That is, if there is a democratic equilibrium with parameters in \( P_1 \) then it must involve zero transfers since a democratic equilibrium either has zero or positive transfers, yet it can not have positive transfers because parameters being in \( P_1 \) preclude them from being in \( P_2 \) (and similarly for the consequences of parameters in \( P_2 \)).

\( \square \)

**Proof of Lemma 4:**

Proof. From (10) we have

\[
\hat{\tau}_T \equiv (1 - \delta) \cdot [\gamma \cdot V_D^L - (\delta \cdot V_D^N + (1 - \delta) \cdot V_D^N)].
\]

The strategy is to show that if tyrants are secure then the value to being a tyrant leader is at least as great as being a leader in democracy and therefore strictly better than being an insider in democracy since \( V_D^L > V_D^N \) (see Result 2).

If a tyrant is secure, then \( c_T = 0 \) and either \( \hat{\tau}_T \leq 0 \) or \( \hat{\tau}_T \in (0, U) \). If \( \hat{\tau}_T \leq 0 \) then \( \tau_T = 0 \) and (13) implies

\[
V_T^L = \frac{F + U}{\delta} = V_D^L + V_D^N > V_D^L > V_D^N
\]

where the second equality comes from adding (11) and (12) and re-arranging. If on the other hand \( \hat{\tau}_T \in (0, U) \), then \( \tau_T = \hat{\tau}_T \) and thus \( V_T^N = \gamma \cdot (1 - \delta) \cdot V_D^L \). Since the right side is the value of holding a coup in democracy, we have \( V_T^N \leq V_D^N \). But then using this in the right side of (14) we have \( V_T^N \geq \tau_T + (1 - \delta) \cdot V_T^N \) so that

\[
\tau_T \leq \delta \cdot V_T^N
\]
Using this in (13) gives \( V_T^L \geq F + U - \delta \cdot V_T^N + (1 - \delta) \cdot V_T^L \), and using \( V_T^N \leq V_D^N \) gives \( V_T^L \geq F + U - \delta \cdot V_D^N + (1 - \delta) \cdot V_T^L \). Therefore we have

\[
V_T^L + V_D^N \geq \frac{F + U}{\delta} = V_D^L + V_D^N.
\]

(37)

Thus \( V_T^L \geq V_D^L > V_D^N \), implying again that election results are not respected. \( \square \)

**Proof of Lemma 5:**

The strategy is to note that a tyrant is insecure only if \( \hat{T} \geq U \) where \( \hat{T} \) is given by (34) where the values of \( \{V_{D_{1}}^L, V_{D_{1}}^N\} \) are given by the solutions to (11) and (12) using \( \tau_D = 0 \) if parameters are in \( P_1 \) and \( \tau_D = \hat{T} \) if parameters are in \( P_2 \) where \( \hat{T} \) is given by (33), and where \( V_{D_{1}}^N = \gamma \cdot (1 - \delta) \cdot V_{D_{1}}^L \) (since the insider is either indifferent to mounting a coup or strictly prefers it).

Using \( V_T^L = \gamma \cdot (1 - \delta) \cdot V_T^L \) in (34) gives:

\[
\hat{T} = (1 - \delta) \cdot \delta \cdot (\gamma \cdot (2 - \delta) \cdot V_D^L - V_D^N).
\]

(38)

If parameters are in \( P_1 \), then we have

\[
V_D^L = \frac{1 - p \cdot (1 - \delta) + \frac{F + U}{(2 - \delta) \cdot (1 - p) + p \cdot \delta}}{(2 - \delta) \cdot (1 - p) + p \cdot \delta},
\]

(39)

\[
V_D^N = \frac{(1 - p) \cdot (1 - \delta) + F + U}{(2 - \delta) \cdot (1 - p) + p \cdot \delta},
\]

(40)

which, when used in (38), makes the requirement that \( \hat{T} \geq U \) equivalent to \( \psi \leq g(p) \).

If instead parameters are in \( P_2 \), then we have

\[
V_D^L = \frac{1}{1 + \gamma \cdot (1 - \delta)} \cdot \frac{F + U}{\delta},
\]

(41)

\[
V_D^N = \frac{\gamma \cdot (1 - \delta)}{1 + \gamma \cdot (1 - \delta)} \cdot \frac{F + U}{\delta},
\]

(42)

which, when used in (38), makes the requirement that \( \hat{T} \geq U \) equivalent to \( \psi \leq \mu_2 \). \( \square \)

**Proof of Proposition 2:**

The ‘only if’ part follows from Lemmas 3 and 5. The strategy for showing the ‘if’ part is to show that elections are respected if tyrants are insecure (and \( \gamma^2 \geq \delta/(1 - \delta)^2 \)).

If \( p \leq p^* \) and \( \psi < g(p) \) or \( p > p^* \) and \( \psi \in [f(p), \mu_2] \), then equilibrium must have \( \hat{T} > U \) (by virtue of \( \psi < g(p) \) and \( \psi < \mu_2 \)). This implies that it is impossible for a tyrant to dissuade a coup, and thus any equilibrium must have \( c_T = 1 \) and \( \tau_T = 0 \). As such, (13) implies that

\[
V_T^L = \frac{F + U}{\delta + \gamma \cdot (1 - \delta)}.
\]

(43)

If \( p > p^* \) and \( \psi \in [f(p), \mu_2] \) (parameters are in \( S_2 \)), then we have \( \tau_D = \hat{T} \) where \( \hat{T} \) is given by (33). This, along with (11) and (12), gives:

\[
V_D^N = \frac{\gamma \cdot (1 - \delta)}{1 + \gamma \cdot (1 - \delta)} \cdot \frac{F + U}{\delta}.
\]

(44)
It then follows that elections are respected (i.e. $V_D^N \geq V_T^L$) if and only if
\[ \frac{\gamma \cdot (1-\delta)}{1 + \gamma \cdot (1-\delta)} \geq \frac{\delta}{\delta + \gamma \cdot (1-\delta)}, \tag{45} \]
which holds if and only if $\gamma^2 \geq \delta/(1-\delta)^2$.

If instead $p \leq p^*$ and $\psi < g(p)$ (parameters are in $S_1$), then we have $\tau_D = 0$ and from (11) and (12) we get:
\[ V_D^N = \frac{(1-p) \cdot (1-\delta)}{(2-\delta) \cdot (1-p) + p \cdot \delta} \cdot \frac{F + U}{\delta}. \tag{46} \]
It then follows that elections are respected (i.e. $V_D^N \geq V_T^L$) if and only if
\[ \frac{(1-p) \cdot (1-\delta)}{(2-\delta) \cdot (1-p) + p \cdot \delta} \geq \frac{\delta}{\delta + \gamma \cdot (1-\delta)}, \tag{47} \]
which is equivalent to
\[ \frac{p}{1-p} \leq \gamma \left( \frac{1-\delta}{\delta} \right)^2 - \frac{1}{\delta}. \tag{48} \]
But note that the left side is increasing in $p$. But since $p \leq p^*$, this condition is satisfied for all $p \leq p^*$ if it is satisfied at $p^*$. Since
\[ \frac{p^*}{1-p^*} = \frac{1-\gamma}{\gamma \cdot \delta}, \tag{49} \]
equation (48) is indeed satisfied at $p = p^*$ if $\gamma^2 \geq \delta/(1-\delta)^2$.

Thus, as long as $\gamma^2 \geq \delta/(1-\delta)^2$ holds, if $p \leq p^*$ and $\psi < g(p)$ or $p > p^*$ and $\psi \in [f(p), \mu_2]$ then a unique equilibrium with the stated properties exists.

The exact same existence arguments apply in the knife-edge cases of $p \leq p^*$ and $\psi = g(p)$ or $p > p^*$ and $\psi = \mu_2$, except that another democratic equilibrium will exist. If $p \leq p^*$ and $\psi = g(p)$ the added equilibrium will have still have zero transfers in the democratic state, but will have $\tau_T = U$ and some $c_T > 0$ in the tyranny state. Similarly, if $p > p^*$ and $\psi = \mu_2$ the added equilibrium will have still have positive transfers in the democratic state, but will have $\tau_T = U$ and some $c_T > 0$ in the tyranny state. This establishes the ‘if’ statement and the generic uniqueness. \hfill \Box

**Proof of Proposition 3:**

*Proof.* This proof follows closely from the proof of proposition 2. Specifically, if $\gamma^2 < \delta/(1-\delta)^2$, then (45) can not hold and as a result a democratic equilibrium can not exist if parameters are in $S_1$. If an equilibrium with parameters in $S_1$ is to exist, then (48) must hold.

Note that the condition is not satisfied for any $p \in [0, 1]$ (implying a democratic equilibrium does not exist) if $\gamma < \delta/(1-\delta)^2$. Intuitively, there is a maximum possible payoff that an insider in democracy can receive and it must be the case that this is larger than the amount an insecure tyrant can obtain. Specifically, the maximum share of total available surplus (i.e. $(F + U)/\delta$) that can accrue to the insider in equilibrium is $(1-\delta)/(2-\delta)$ (corresponding to $p = 0$). This maximum share is decreasing in $\delta$. The amount that an insecure tyrant is able to secure is decreasing in $\gamma$ as coups become less of a threat. Thus, the existence of a democratic equilibrium is jeopardized when $\gamma$ is relatively low (and/or when $\delta$ is relatively high). \hfill \Box
Proof of Proposition 4:

Proof. Suppose to the contrary that such an equilibrium did exist. Let \( H^{eqm} \) be the set of histories on the equilibrium path, \( H^{coup} \) be the set of histories at which equilibrium strategies call for a coup (such histories need not be on the equilibrium path), and \( H^{eqm} \equiv H^{eqm} \setminus H^{coup} \) be the set of histories that are on the equilibrium path but do not call for a coup. Let \( V^{coup}(h) \) denote the continuation value associated with holding a coup at history \( h \), and let \( V^{NP}(h) \) be the value of being the insider at history \( h \) under the proposed equilibrium strategies.

The *coup symmetry* property states that there exists histories \( h' \in H^{eqm} \) and \( h'' \in H^{coup} \) such that

\[
V^{coup}(h') \geq V^{NP}(h'').
\]  
(50)

Since equilibrium strategies call for a coup at history \( h'' \), the leader would strictly prefer to commence play as if they were at any history in \( H^{eqm} \). Thus, in order to be renegotiation-proof, it must be that the insider at history \( h'' \) strictly prefers to undertake the (disciplining) coup over commencing play as if they were at any history in \( H^{eqm} \). That is,

\[
V^{NP}(h'') > \max_{h \in H^{eqm}} V^{NP}(h).
\]  
(51)

But equations (50) and (51), together with the fact that \( \max_{h \in H^{eqm}} V^{NP}(h) \geq V^{NP}(h') \) by virtue of \( h' \in H^{eqm} \), gives us

\[
V^{coup}(h') > V^{NP}(h'),
\]  
(52)

which is a contradiction since it implies that the insider at history \( h' \) is not best-responding by following the equilibrium strategy of not mounting a coup.

Proof of Proposition 5:

Proof. Let \( V^{NP}_p(h) \) represent the value of being an insider in a power-sharing equilibrium at history \( h \), and recall that \( H^{coup} \) is the set of histories at which equilibrium strategies call for a coup. The equilibrium will fail to be renegotiation-proof if there exists histories \( h \) and \( h' \in H^{coup} \) such that \( V^{NP}_p(h) \geq V^{NP}_p(h') \). Intuitively, at \( h' \) the insider is required to mount a coup and they must be unwilling to commence with play according to equilibrium strategies from any history \( h \) (since such play constitutes an equilibrium by sub-game perfection). Note that \( h \) need not be on the equilibrium path.

We first derive a bound, \( V^{N}_p \), such that there always exists a history \( h \) for which \( V^{NP}_p(h) \geq V^{N}_p \). This bound turns out to be the value of being an insider in the minimalist democracy when zero transfers are made (i.e. in region \( S_1 \)). That is,

\[
V^{N}_p \equiv \frac{(1 - p) \cdot (1 - \delta) \cdot F + U}{1 - (1 - \delta)(2p - 1) \cdot \delta}.
\]  
(53)

To see why this is so, suppose to the contrary that \( V^{NP}_p(h) < V^{N}_p \) for all \( h \). Then for all \( h \) on the equilibrium path we have

\[
V^{NP}_p(h) = \tau(h) + (1 - \delta) \cdot (p \cdot V^{N}_p(h^-) + (1 - p) \cdot V^{L}_p(h^+)),
\]  
(54)
where \(h^- (h^+)\) is the history following \(h\) in which the insider does not die and the leader (insider) wins the election. Since \(V_p^N(h) + V_p(h) = V_D \equiv (F + U)/\delta\) for all \(h\) on the equilibrium path, we have

\[ V_p^N(h) = \tau(h) + (1 - \delta) \cdot (p \cdot V_p^N(h^-) + (1 - p) \cdot [V_D - V_p^N(h^+)]) \tag{55} \]

Since \(\tau(h) \geq 0\), and \(V_p^N(h^+) < V_p^N\) by supposition, we have

\[ V_p^N(h) > (1 - \delta) \cdot (1 - p) \cdot [V_D - V_p^N] + (1 - \delta) \cdot p \cdot V_p^N(h^-) \tag{56} \]

But this implies an upper bound, \(\bar{V}_p^N\), whereby \(V_p^N(h) > \bar{V}_p^N\) for all \(h\) on the equilibrium path. This bound is the value of \(\bar{V}_p^N\) which satisfies

\[ \bar{V}_p^N = (1 - \delta) \cdot (1 - p) \cdot [V_D - V_p^N] + (1 - \delta) \cdot p \cdot \bar{V}_p^N. \tag{57} \]

But it is straightforward to verify that \(\bar{V}_p^N = V_p^N\) where \(V_p^N\) is defined in (53). This implies \(V_p^N = \bar{V}_p^N < V_p^N(h) < V_p^N\) which is a contradiction.

We now derive an upper bound, \(\bar{V}_p^N\), whereby \(V_p^N(h') \leq \bar{V}_p^N\) for all \(h' \in H^{coup}\). That is, an upper bound on the value of mounting a coup when the equilibrium strategy calls for it. Start by noting that the value of being a leader is bounded below by the value of keeping all patronage and facing coups with probability one each period. Denote this value \(\bar{V}_p^N\) and note that it corresponds to the value of being a strongly insecure autocrat or tyrant: \(\bar{V}_p^N \equiv (F + U)/(1 - (1 - \gamma)(1 - \delta))\). Thus the value of being an insider (on or off the path) is bounded below by \(V_p^N \equiv \gamma \cdot (1 - \delta) \cdot \bar{V}_p^N\). Since the total value of office is bounded above by \((F + U)/\delta\), it follows that the value of being a leader is bounded above by \(\bar{V}_p^N \equiv (F + U)/\delta - V_p^N\). Since this is the very best that one can obtain from a successful coup, for all \(h' \in H^{coup}\) we have

\[ V_p^N(h') \leq \bar{V}_p^N \equiv \gamma \cdot (1 - \delta) \cdot \bar{V}_p^N \leq \frac{\gamma (1 - \delta)}{\delta + \gamma (1 - \delta)^2} \cdot \frac{F + U}{\delta}. \]

Given these bounds, it follows that the equilibrium must fail to be renegotiation-proof if \(\bar{V}_p^N < \bar{V}_p^N\). That is, there must exist histories \(h\) and \(h' \in H^{coup}\) such that \(V_p^N(h') < V_p^N(h)\). Thus the equilibrium must fail to be renegotiation-proof if

\[ \frac{(1 - \delta)(1 - p)}{2 - \delta(1 - p) + p \cdot \delta} \geq \frac{\gamma(1 - \delta)}{\delta + \gamma(1 - \delta)} \cdot [\delta + \gamma(1 - \delta)^2] \tag{58} \]

Since the left side is strictly decreasing in \(p\), this holds for \(p \leq p^*\) where \(p^*\) is the value of \(p\) that makes the above hold with equality. Such a value will clearly only depend on \((\delta, \gamma)\). Since the left side is independent of \(\gamma\) and strictly decreasing in \(p\) whereas the right side is strictly increasing in \(\gamma\), it follows (implicit function theorem) that \(p\) is strictly decreasing in \(\gamma\).

Note that we always have \(p^* < 1\), since the left side is zero at \(p = 1\) whereas the right side is positive. Note also that \(p^* > 0\) if \(\gamma < 1/2\). Since the right side is increasing in \(\gamma\), the fact that \(\gamma < 1/2\) implies that the right side is less than the right side evaluated at \(\gamma = 1/2\): i.e. \((1/2)(1 - \delta)(1 + \delta)/(1 + \delta)\). But the value of the left side at \(p = 0\) is \((1 - \delta)/(2 - \delta)\), which is greater than \((1/2)(1 - \delta)(1 + \delta)/(1 + \delta)\). Thus \(p^* > 0\) if \(\gamma < 1/2\). Thus, \(p^* \in (0, 1)\) if \(\gamma < 1/2\).

**Corollary 1.** If \(\gamma \in \left(\frac{\delta}{1 + \delta}, \frac{1}{2}\right]\), then there exists parameters for which a minimalist democracy exists yet a renegotiation-proof power-sharing equilibrium does not exist.

**Proof.** If \(g(0) \geq 0\), then there exists parameters (specifically \(\psi = 0\)) such that a minimalist democracy equilibrium exists for all \(p\). It is straightforward to verify that \(g(0) \geq 0\) if and only if
\[ \gamma \geq \frac{\delta}{2 - \delta}. \] From proposition 5, we know that \( p^{**} > 0 \) if \( \gamma < 1/2 \). Thus, for values of \( p \in [0, p^{**}] \) take \( \psi = 0 \) so that a minimalist democracy equilibrium exists yet a renegotiation-proof power-sharing equilibrium does not.

**Proof of Proposition 6:**

**Proof.** From lemma 5, the existence of democratic equilibrium implies \( \psi \leq \mu_2 \) (since \( g \) is increasing in \( p \) with \( g(p^*) = \mu_2 \)). Thus, whenever a democratic equilibrium exists, we have \( V_A^N = \gamma \cdot (1 - \delta) \cdot V_A^L \). Since \( \gamma \cdot (1 - \delta) \cdot V_A^L \leq V_D^N \) (no coups) we have that \( V_A^L < V_D^L \Rightarrow V_A^N < V_D^N \): i.e. insiders strictly prefer democracy to autocracy whenever leaders do. Thus, for the strict inequality claims, it is sufficient to show that \( V_A^L < V_D^L \) when \( \psi < \mu_2 \).

If \( \psi \in [0, \mu_1] \), then the result follows since \( V_A^L = V_D^L \leq V_D^N < V_D^L \). The equality follows since the autocrat is strongly insecure, the weak inequality follows from the self-enforcing condition, and the strict inequality is readily computed from the value functions.

If \( \psi \in (\mu_1, \mu_2) \), then

\[ \hat{\tau}_A = U \leq \hat{\tau}_T, \]  \hspace{1cm} (59)

with strict inequality if parameters are in \( P_2 \). The equality follows from the autocrat being weakly insecure and the inequality follows from a tyrant necessarily being insecure (strictly so if in \( P_2 \)). Furthermore,

\[ \hat{\tau}_T \leq (1 - \delta) \cdot \delta \cdot \gamma \cdot V_D^L, \]  \hspace{1cm} (60)

with strict inequality if parameters are in \( P_1 \). This follows because the fact that \( V_D^N = \gamma \cdot (1 - \delta) \cdot V_D^L \leq V_D^N \) implies \( \hat{\tau}_T \equiv (1 - \delta) \cdot \gamma \cdot V_D^L \). The inequality is strict if in \( P_1 \). Finally,

\[ \hat{\tau}_A = (1 - \delta) \cdot \delta \cdot \gamma \cdot V_A^L. \]  \hspace{1cm} (61)

This follows because \( V_A^N = \gamma \cdot (1 - \delta) \cdot V_A^L \) implies \( \hat{\tau}_A \equiv (1 - \delta) \cdot \gamma \cdot V_A^L \). But then using (59)-(61) gives

\[ (1 - \delta) \cdot \delta \cdot \gamma \cdot V_A^L = \hat{\tau}_A = U \leq \hat{\tau}_T \leq (1 - \delta) \cdot \delta \cdot \gamma \cdot V_D^L, \]  \hspace{1cm} (62)

implying that \( V_A^L < V_D^L \) as required. This is because the first inequality is strict if parameters are in \( P_2 \) and the second inequality is strict if parameters are in \( P_1 \).

If \( \psi = \mu_2 \), then the existence of a democratic equilibrium implies that we are in region \( P_2 \). Thus the no-coup constraint holds with equality: \( \gamma \cdot (1 - \delta) \cdot V_D^L = V_D^N \). But then the fact that \( V_D^N = \gamma \cdot (1 - \delta) \cdot V_A^L \) implies that \( V_A^L = V_D^L \Rightarrow V_A^N = V_D^N \). To show that \( V_A^L = V_D^L \) when parameters are in \( P_2 \) and \( \psi = \mu_2 \), an argument similar to the one above can be used, noting that (59) holds with equality when \( \psi = \mu_2 \) and (60) holds with equality when parameters are in \( P_2 \). \qed

**References**


